

Principles of Robot Autonomy II

Human-Robot Interaction



Stanford
University



Recap

- Imitation learning and inverse RL
- Learning from other sources of data – Pairwise Comparisons
- Learning from other sources of data – Foundation Models
- Learning from physical feedback
- Learning from gestures
- Learning from sketches
- Data Quality

Types of Imitation Learning

Behavioral Cloning

$$\arg \min_{\theta} \mathbb{E}_{(s, a^*) \sim P^*} L(a^*, \pi_{\theta}(s))$$

Works well when P^* is close to P_{θ}

Direct Policy Learning (via Interactive Demonstrator)

Requires Interactive Demonstrator (BC is a 1-step special case)

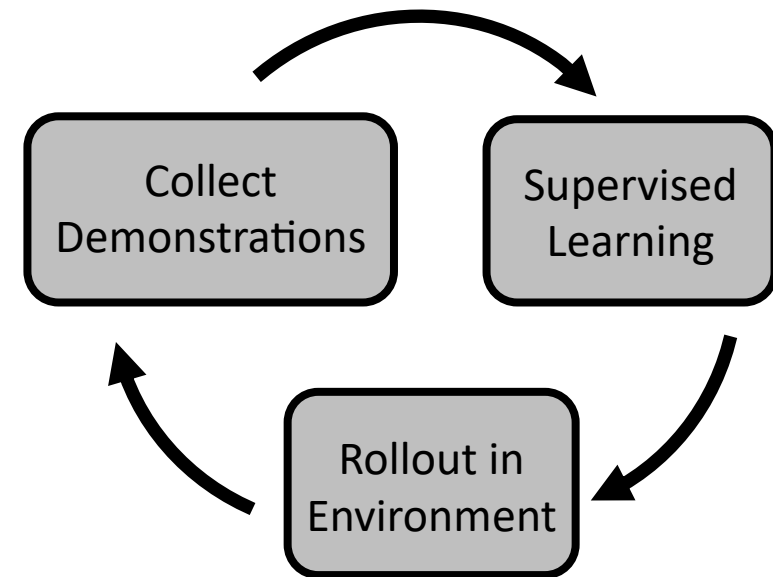
Inverse RL

Learn r such that:

$$\pi^* = \arg \max_{\theta} \mathbb{E}_{s \sim P(s|\theta)} r(s, \pi_{\theta}(s))$$

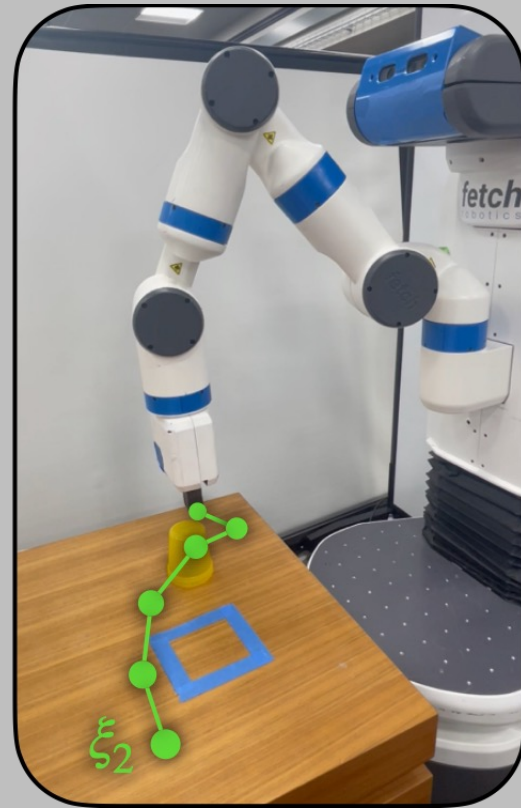
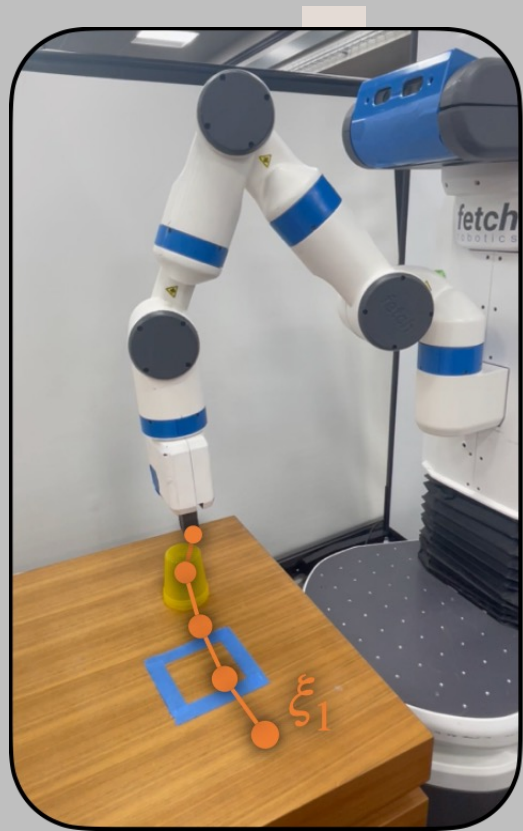
RL problem

Assume learning r is statistically easier than directly learning π^*

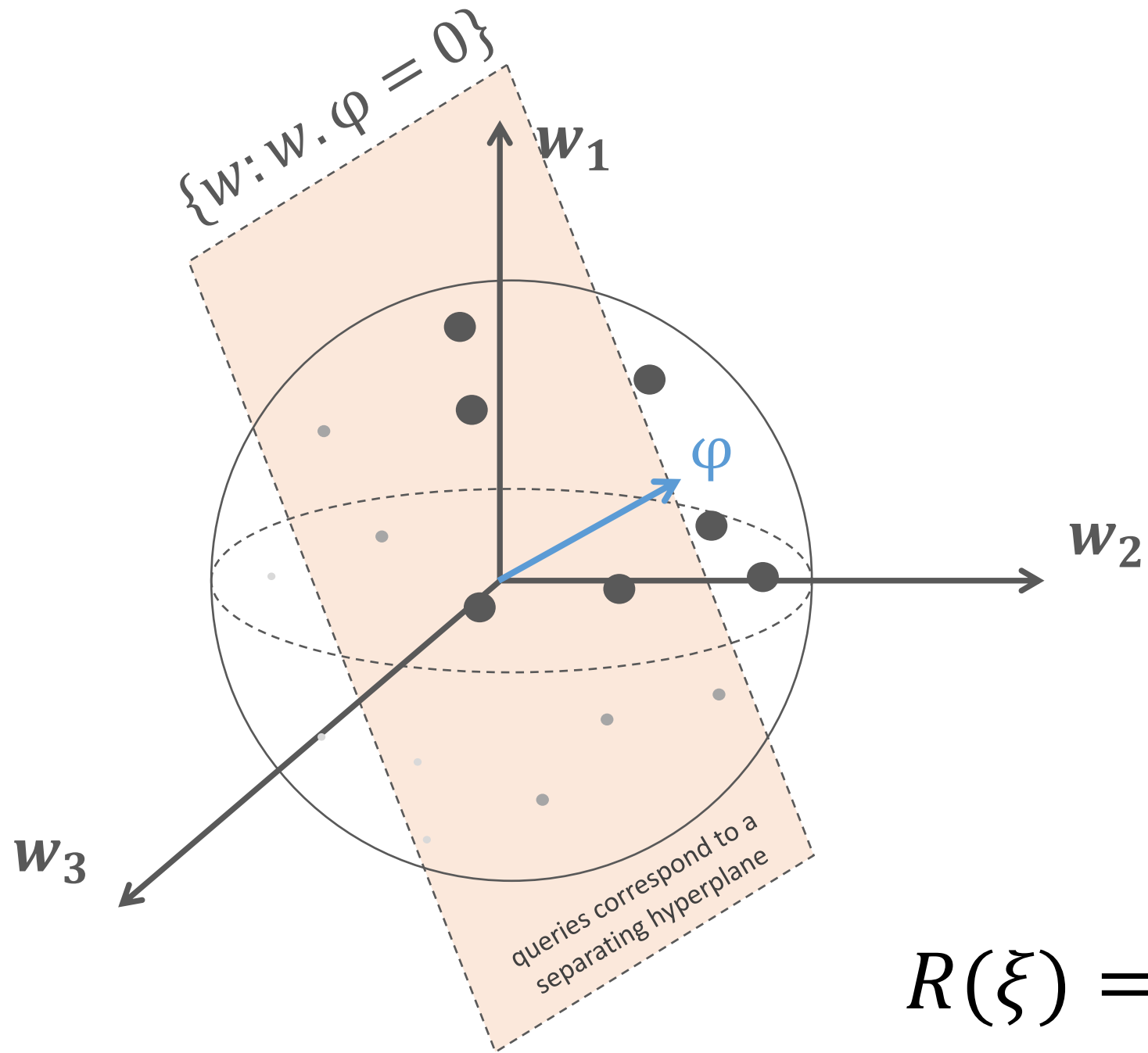


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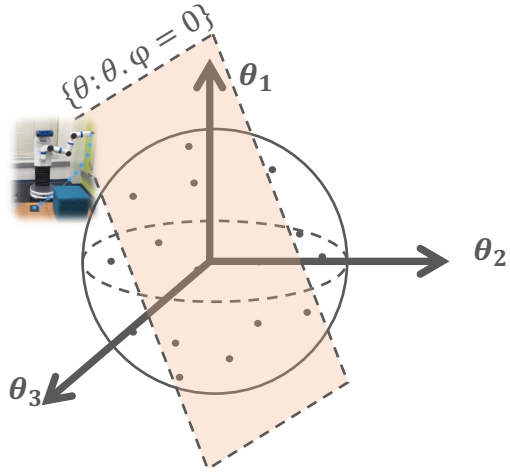


ξ_A or ξ_B ?



$$R(\xi) = w \cdot \phi(\xi)$$

Actively synthesizing queries



minimum volume removed

$$\max_{\varphi} \min\{\mathbb{E}[1 - f_{\varphi}(w)], \mathbb{E}[1 - f_{-\varphi}(w)]\}$$

Subject to $\varphi \in \mathbb{F}$

$$\mathbb{F} = \{\varphi: \varphi = \Phi(\xi_A) - \Phi(\xi_B), \xi_A, \xi_B \in \Xi\}$$

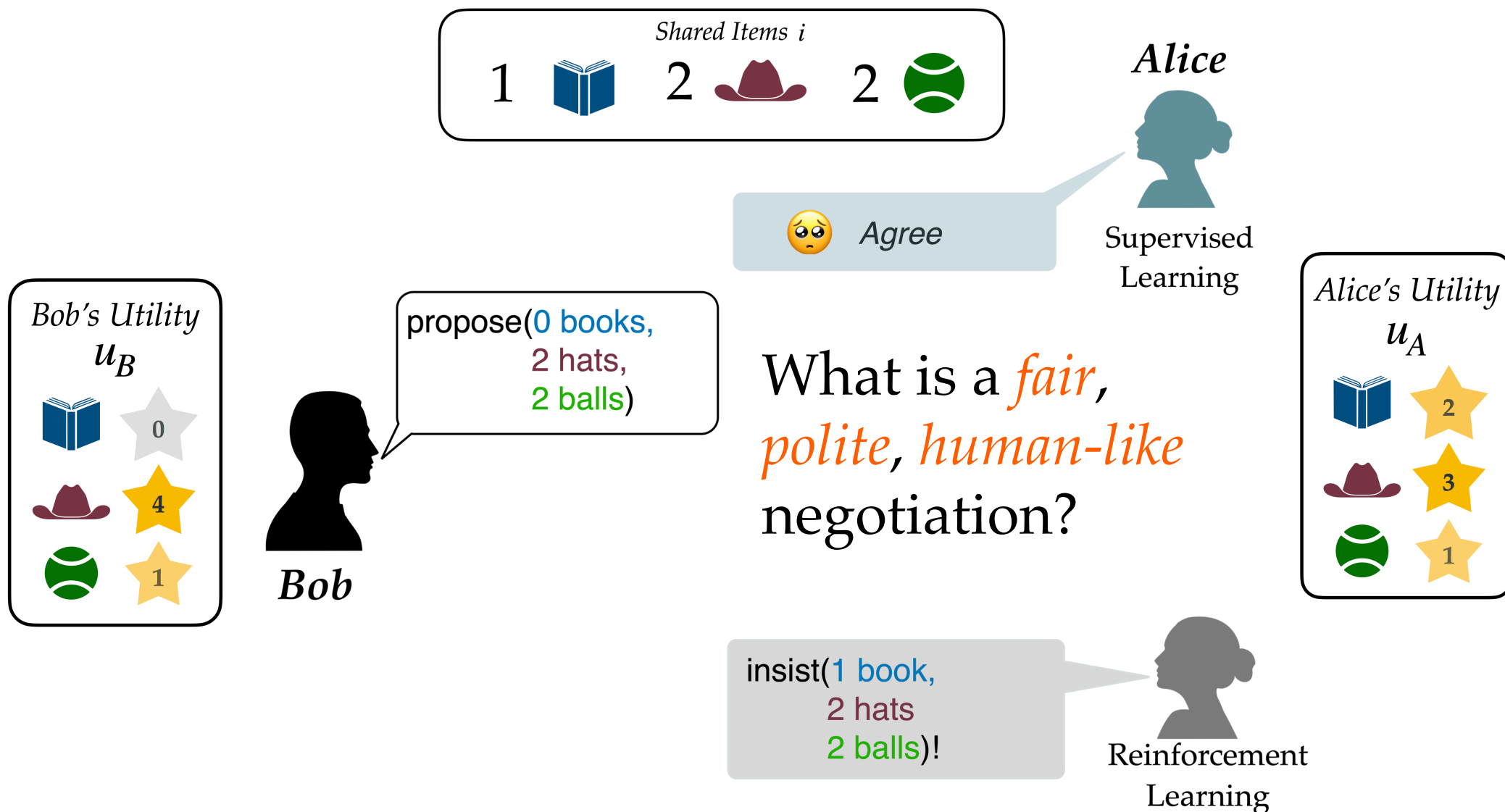
Human update function $f_{\varphi}(w) = \min(1, \exp(I_t w^T \varphi))$

- [Sadigh et al. RSS17]
- [Biyik et al. CoRL18]
- [Biyik et al. CDC19]
- [Palan et al. RSS19]
- [Biyik et al. CoRL19]
- [Basu et al. IROS19]
- [Biyik et al. RSS20]
- [Myers et al. CoRL21]
- [Myers et al. ICRA22]

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Negotiation Domain



Prompt (ρ)

Task description (ρ_1)



Example from user describing objective (versatile behavior) (ρ_2)



Episode outcome described as string using parse f (ρ_3)

Question (ρ_4)

Alice and Bob are negotiating how to split a set of books, hats, and balls.

Alice : propose: book=1 hat=1 ball=0
Bob : propose: book=0 hat=1 ball=0
Alice : propose: book=1 hat=0 ball=1

Agreement!
Alice : 4 points
Bob : 5 points

Is Alice a versatile negotiator?
Yes, because she suggested different proposals.

Alice : propose: book=1 hat=1 ball=0
Bob : propose: book=0 hat=1 ball=0
Alice : propose: book=1 hat=1 ball=0

Agreement!
Alice : 5 points
Bob : 5 points

Is Alice a versatile negotiator?

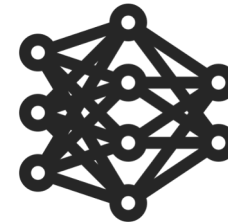
(1) Feed prompt (ρ)

LLM

(2) LLM provides textual output

"No"

(3) Convert to int "0" using parse g and use as reward signal



(4) Update agent (Alice) weights and run an episode

Construct prompt (ρ)

(5) Summarize episode outcome as string (ρ_3) using parser f

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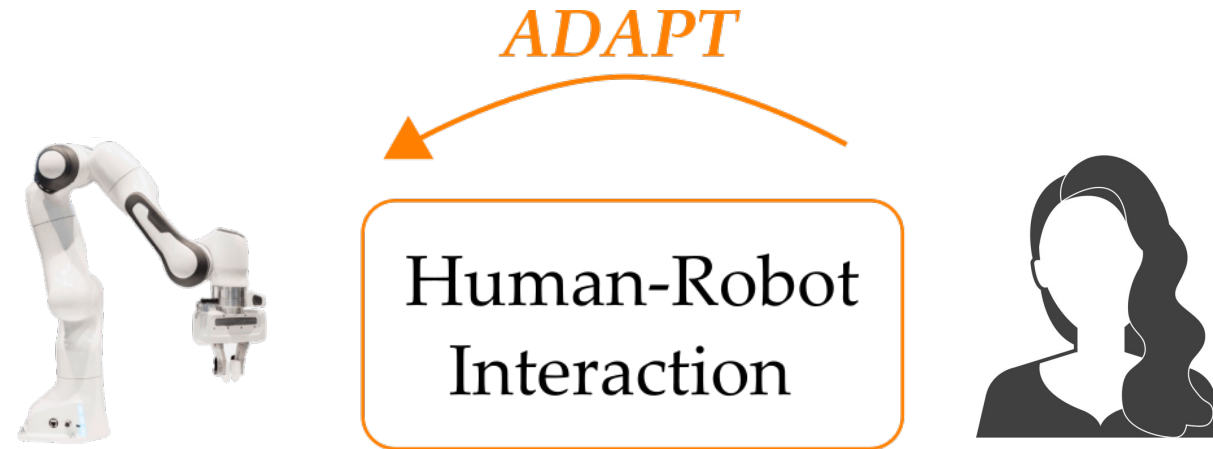
Today's itinerary

- Game-Theoretic Views on Multi-Agent Interactions
- Partner Modeling: Active Info Gathering over Human's Intent
- Partner Modeling: Learning and Influencing Latent Intent
- Partner Modeling: Role Assignment

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- Game-Theoretic Views on Multi-Agent Interactions
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- Partner Modeling: Role Assignment

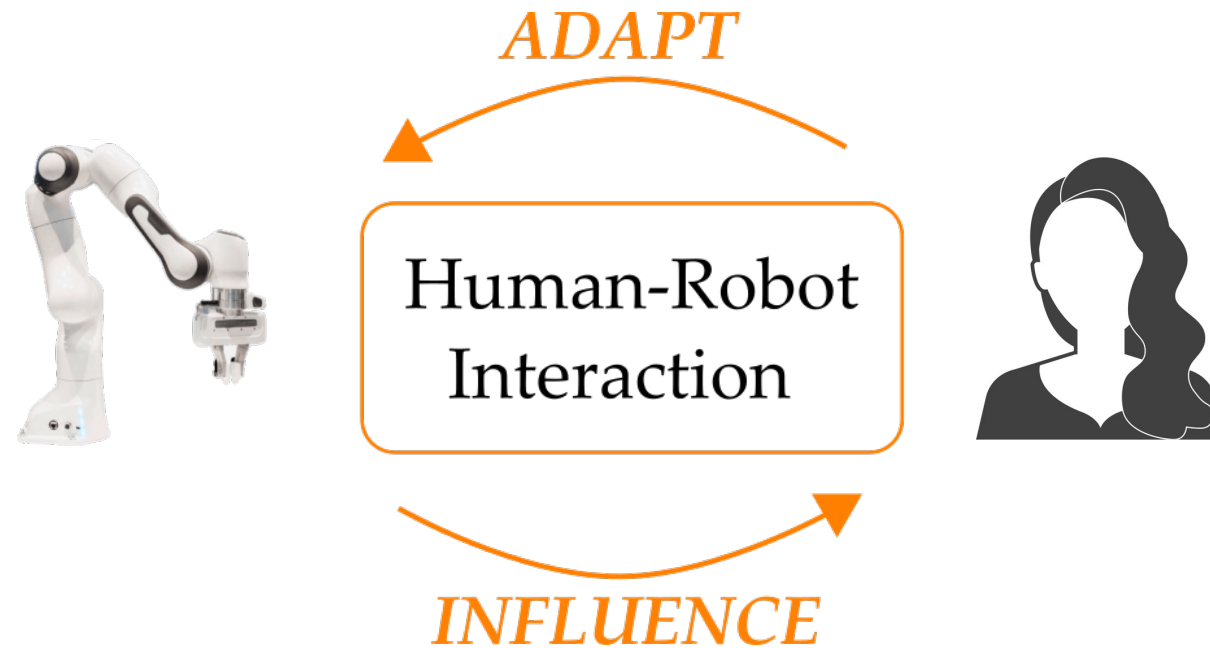
Learning from Humans



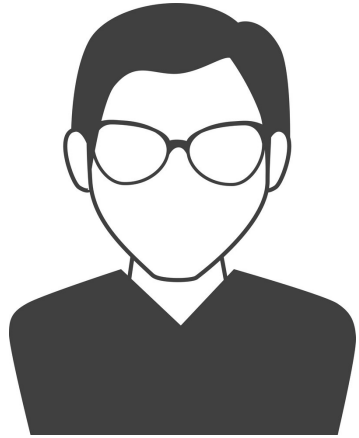
Existing research explores how robots *adapt* to humans

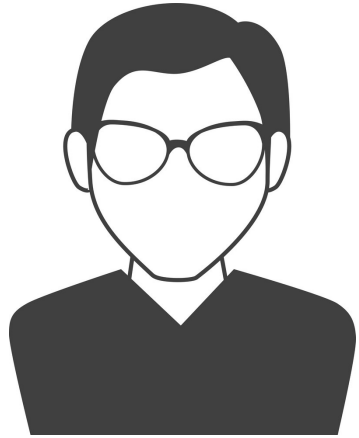
- Imitation learning
- Learning from demonstrations

Influencing Humans

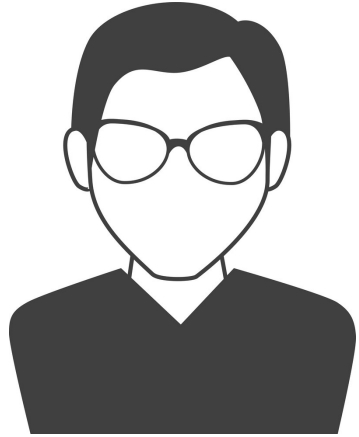


Far less studies how robots *influence* humans

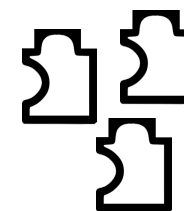
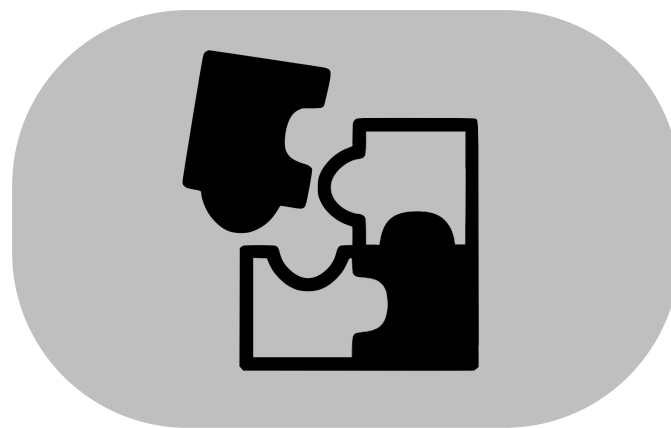
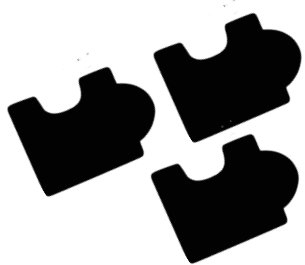




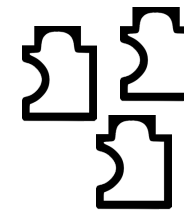
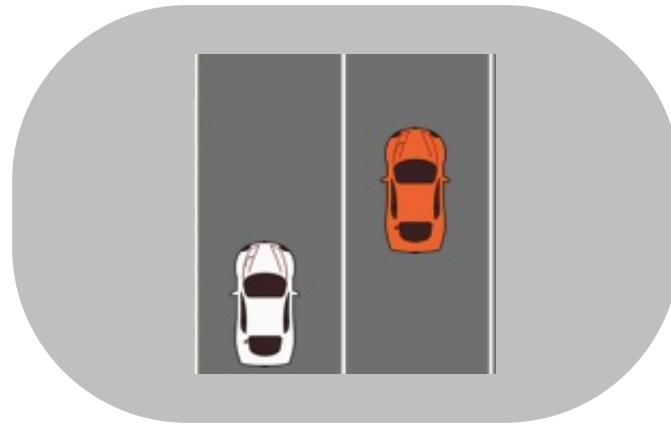
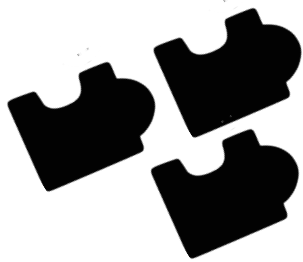
Nth order Theory of Mind

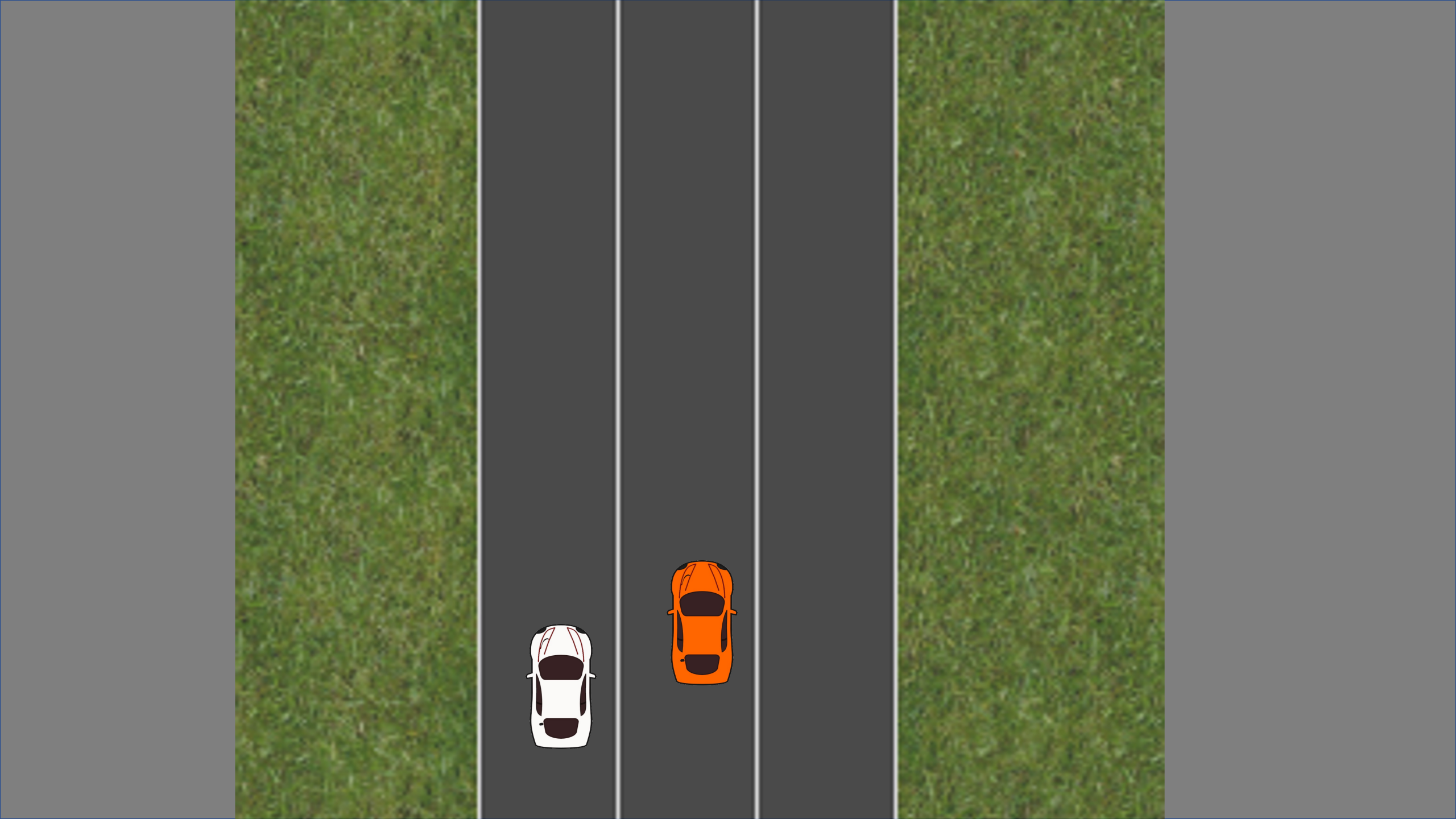


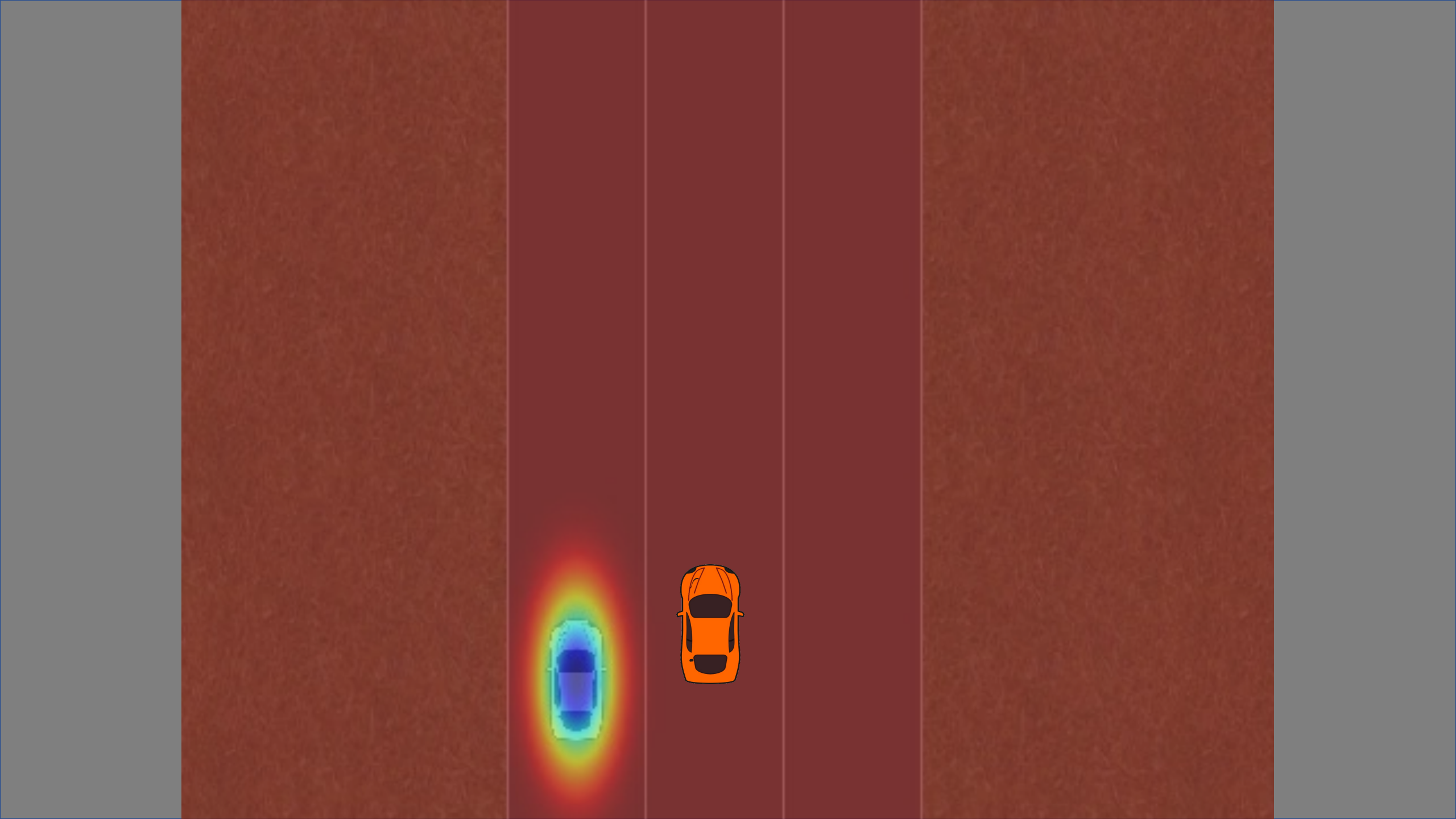
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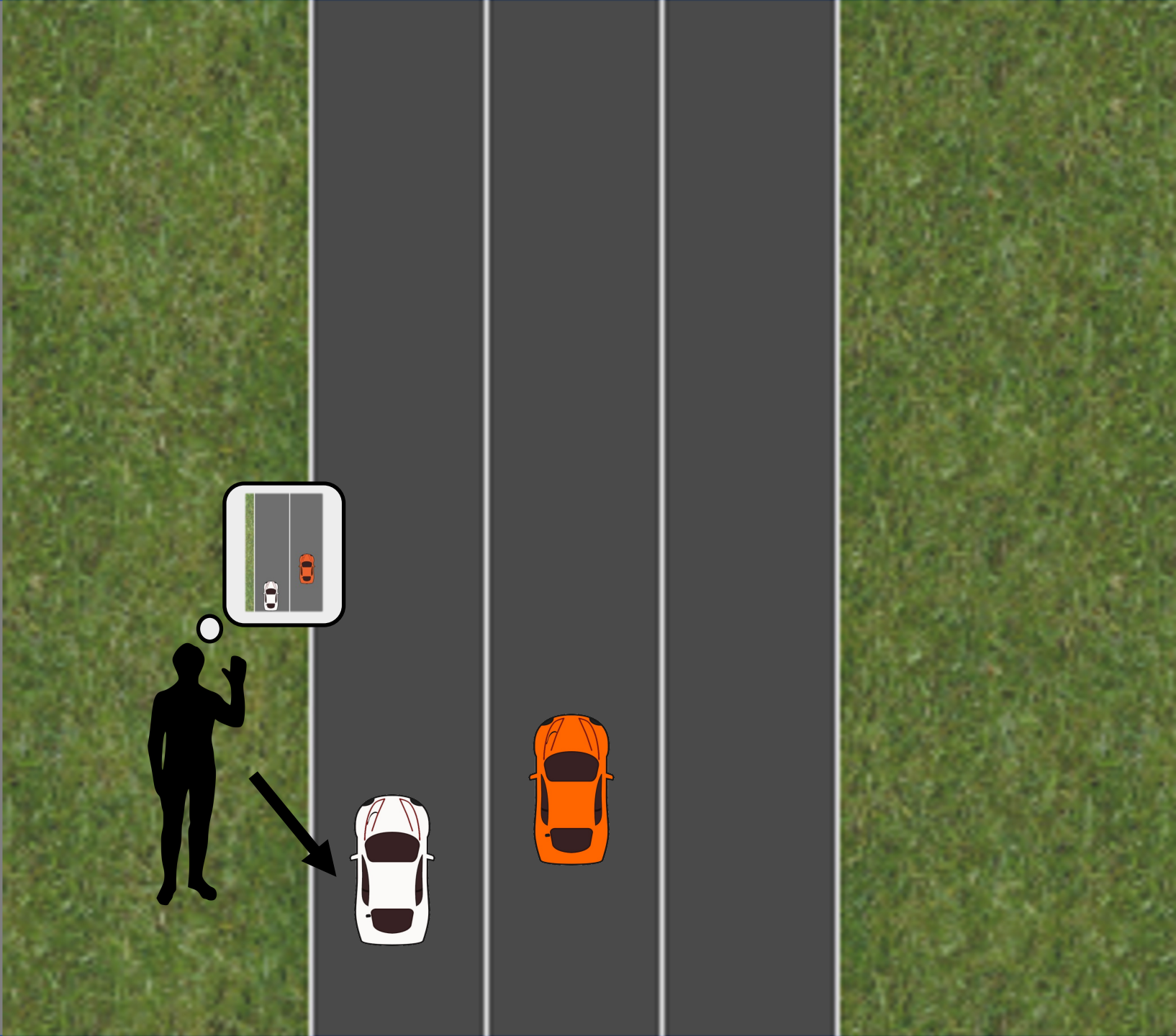


Nth order Theory of Mind









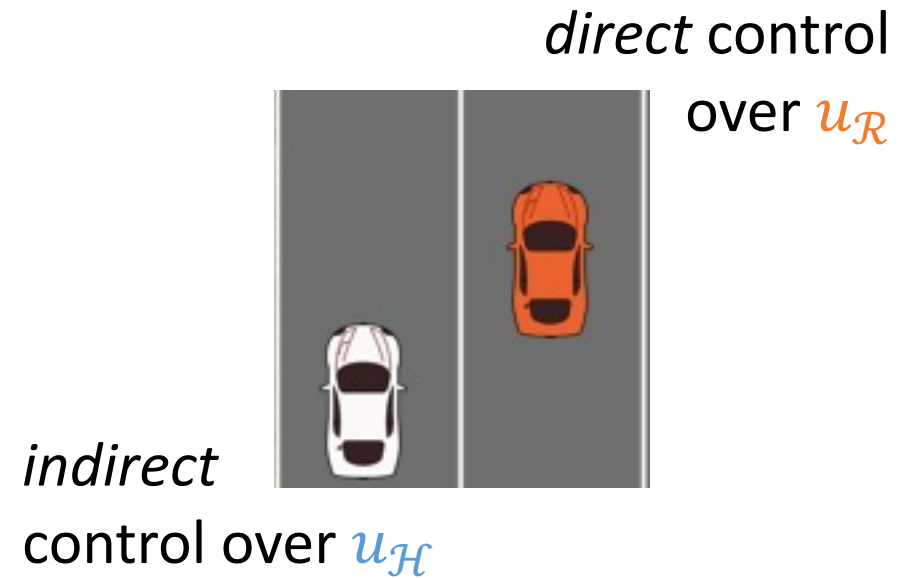
An autonomous car's actions will *affect* the actions of other drivers.





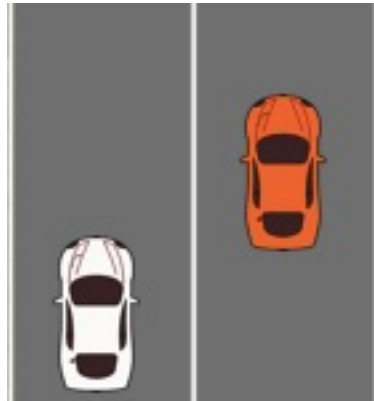
Source: <https://twitter.com/nitguptaa/>

Interaction as a Dynamical System



Interaction as a Dynamical System

$$u_{\mathcal{R}}^* = \operatorname{argmax}_{u_{\mathcal{R}}} R_{\mathcal{R}}(x, u_{\mathcal{R}}, u_{\mathcal{H}}^*(x, u_{\mathcal{R}}))$$



Find optimal actions for the robot while accounting for the human response $u_{\mathcal{H}}^*$.

Model $u_{\mathcal{H}}^*$ as optimizing the human reward function $R_{\mathcal{H}}$.

$$u_{\mathcal{H}}^*(x, u_{\mathcal{R}}) \approx \operatorname{argmax}_{u_{\mathcal{H}}} R_{\mathcal{H}}(x, u_{\mathcal{R}}, u_{\mathcal{H}})$$

Learning Driver Models

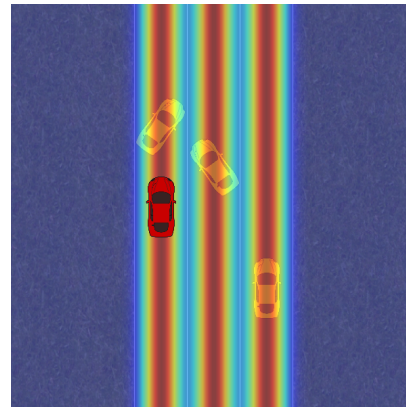
Learn Human's reward function based on Inverse Reinforcement Learning:

$$P(u_{\mathcal{H}}|x, w) = \frac{\exp(R_{\mathcal{H}}(x, u_{\mathcal{R}}, u_{\mathcal{H}}))}{\int \exp(R_{\mathcal{H}}(x, u_{\mathcal{R}}, \check{u}_{\mathcal{H}})) d \check{u}_{\mathcal{H}}}$$

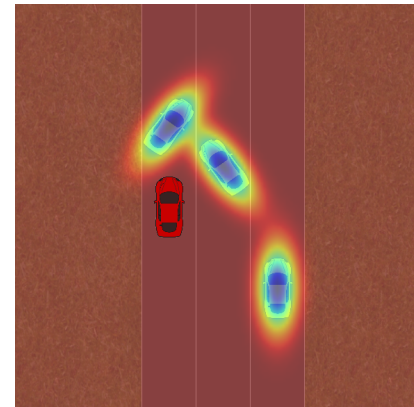
$$R_{\mathcal{H}}(x, u_{\mathcal{R}}, u_{\mathcal{H}}) = w^{\top} \phi(x, u_{\mathcal{R}}, u_{\mathcal{H}})$$



Features for the boundaries of the road.



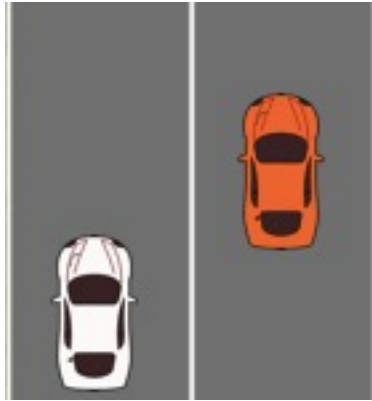
Features for staying inside the lanes.



Features for avoiding other vehicles.

Interaction as a Dynamical System

$$u_{\mathcal{R}}^* = \operatorname{argmax}_{u_{\mathcal{R}}} R_{\mathcal{R}}(x, u_{\mathcal{R}}, u_{\mathcal{H}}^*(x, u_{\mathcal{R}}))$$



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Approximations for Tractability

- Receding Horizon Control:

Plan for short time horizon, replan at every step.

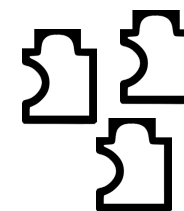
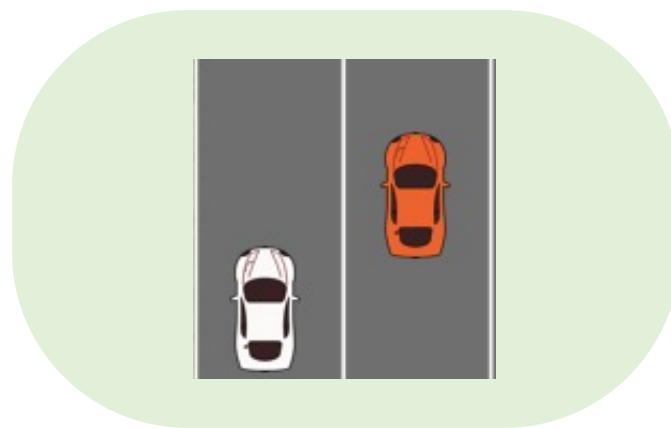
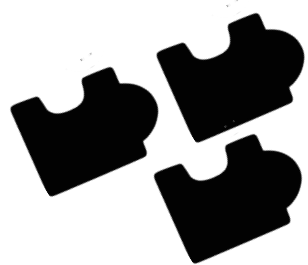
- Model the problem as a *Stackelberg game*.

Give the human full access to $u_{\mathcal{R}}$ for the short time horizon.

Nth order Theory of Mind



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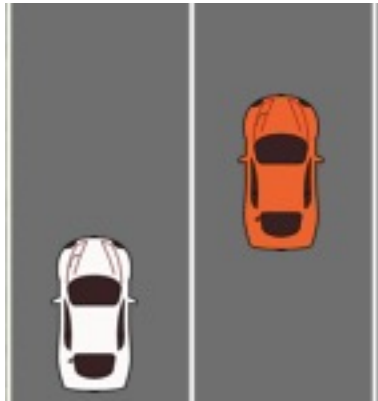
$$u_{\mathcal{H}}^*(x, u_{\mathcal{R}}) = \operatorname{argmax}_{u_{\mathcal{H}}} R_{\mathcal{H}}(x, u_{\mathcal{R}}, u_{\mathcal{H}})$$

- Assume deterministic human model.

Solution of Nested Optimization

$$u_{\mathcal{R}}^* = \operatorname{argmax}_{u_{\mathcal{R}}} R_{\mathcal{R}}(x, u_{\mathcal{R}}, u_{\mathcal{H}}^*(x, u_{\mathcal{R}}))$$

$$R_{\mathcal{R}}(x, u_{\mathcal{R}}, u_{\mathcal{H}}) = \sum_{t=1}^N r_{\mathcal{R}}(x^t, u_{\mathcal{R}}^t, u_{\mathcal{H}}^t)$$



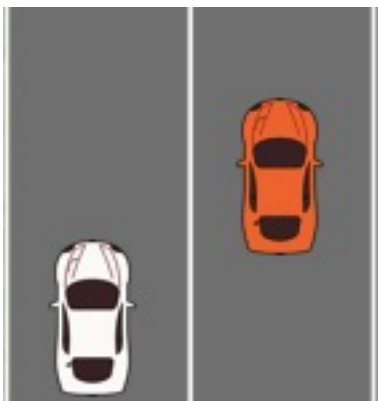
Gradient-Based Method (Quasi-Newton):

$$\left\{ \begin{array}{l} R_{\mathcal{R}}(x, u_{\mathcal{R}}, u_{\mathcal{H}}^*) \\ \frac{\partial R_{\mathcal{R}}}{\partial u_{\mathcal{R}}} = \frac{\partial R_{\mathcal{R}}}{\partial u_{\mathcal{H}}} \frac{\partial u_{\mathcal{H}}^*}{\partial u_{\mathcal{R}}} + \frac{\partial R_{\mathcal{R}}}{\partial u_{\mathcal{R}}} \end{array} \right.$$

$$u_{\mathcal{H}}^*(x, u_{\mathcal{R}}) \approx \operatorname{argmax}_{u_{\mathcal{H}}} R_{\mathcal{H}}(x, u_{\mathcal{R}}, u_{\mathcal{H}})$$

$$R_{\mathcal{H}}(x, u_{\mathcal{R}}, u_{\mathcal{H}}) = \sum_{t=1}^N r_{\mathcal{H}}(x^t, u_{\mathcal{R}}^t, u_{\mathcal{H}}^t)$$

Solution of Nested Optimization



Given $R_{\mathcal{H}}$ is:

- smooth,
 - its minimum is attained,
- for an *unconstrained optimization*, the partial $\frac{\partial R_{\mathcal{H}}}{\partial u_{\mathcal{H}}}$ at the optimum $u_{\mathcal{H}}^*$ evaluates to zero.

Quasi-Newton method:

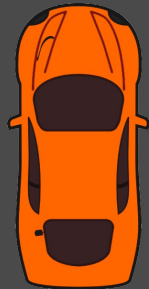
$$\frac{\partial R_{\mathcal{R}}}{\partial u_{\mathcal{R}}} = \frac{\partial R_{\mathcal{R}}}{\partial u_{\mathcal{H}}} \cdot \frac{\partial u_{\mathcal{H}}^*}{\partial u_{\mathcal{R}}} + \frac{\partial R_{\mathcal{R}}}{\partial u_{\mathcal{R}}}$$

$$\frac{\partial R_{\mathcal{H}}}{\partial u_{\mathcal{H}}}(x, u_{\mathcal{R}}, u_{\mathcal{H}}^*(x, u_{\mathcal{R}})) = 0$$

$$\frac{\partial^2 R_{\mathcal{H}}}{\partial u_{\mathcal{H}}^2} \cdot \frac{\partial u_{\mathcal{H}}^*}{\partial u_{\mathcal{R}}} + \frac{\partial^2 R_{\mathcal{H}}}{\partial u_{\mathcal{H}} \partial u_{\mathcal{R}}} \cdot \frac{\partial u_{\mathcal{R}}}{\partial u_{\mathcal{R}}} = 0$$

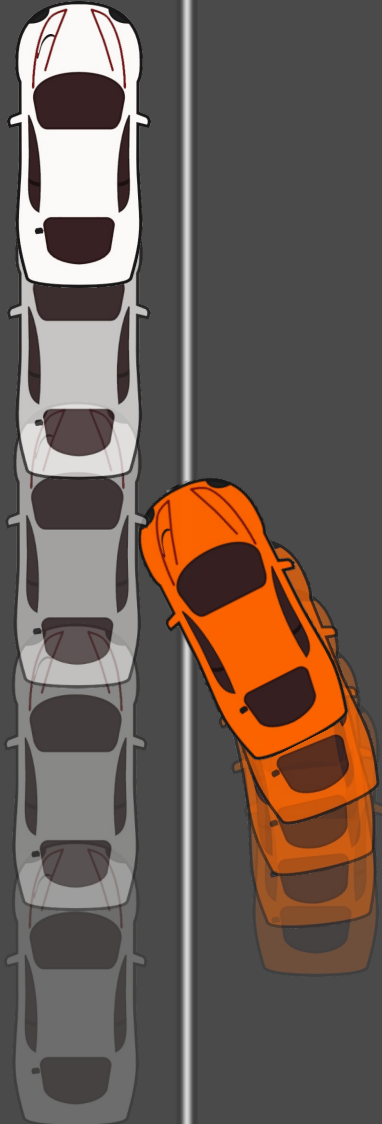
Implication: Efficiency

Human

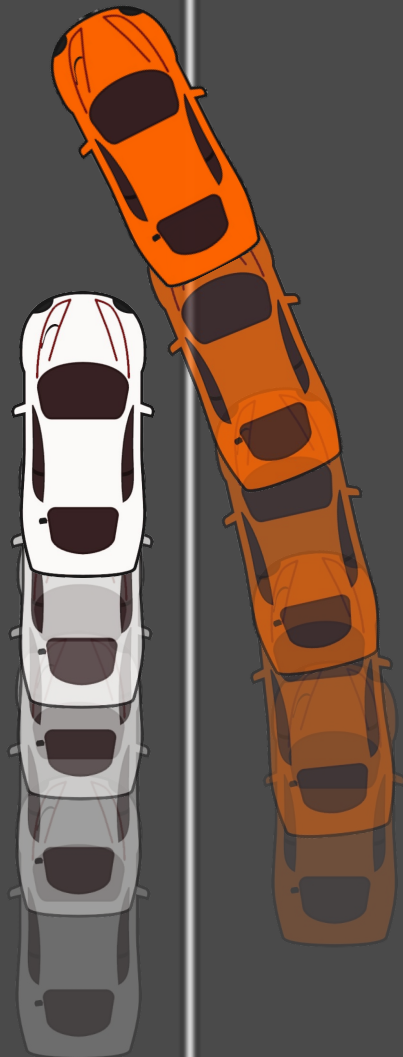


Robot

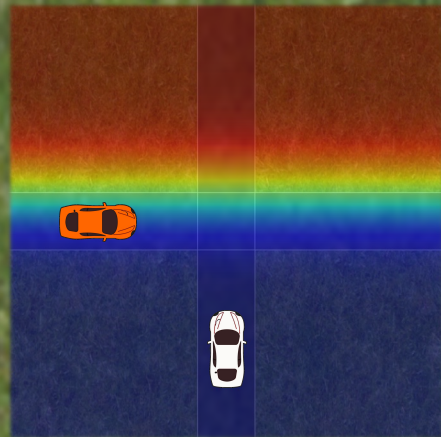
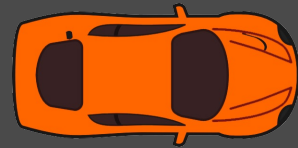
Implication: Efficiency



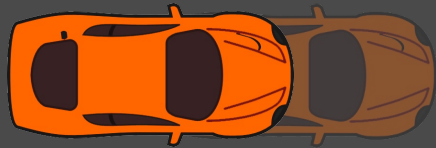
Implication: Efficiency



Implication: Coordination

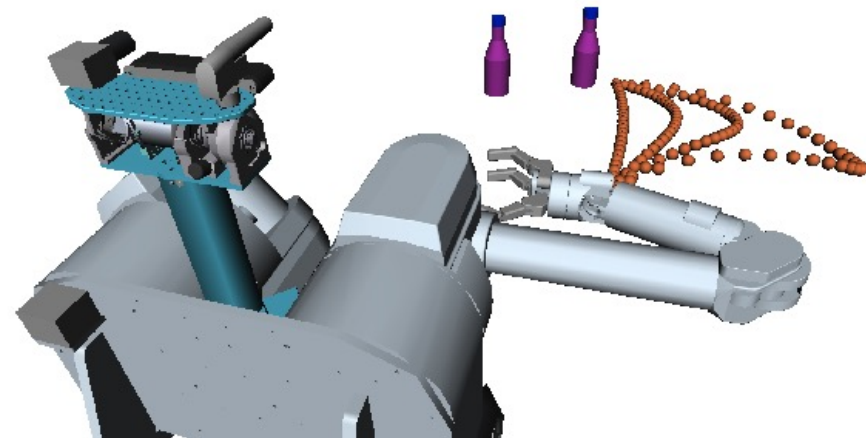
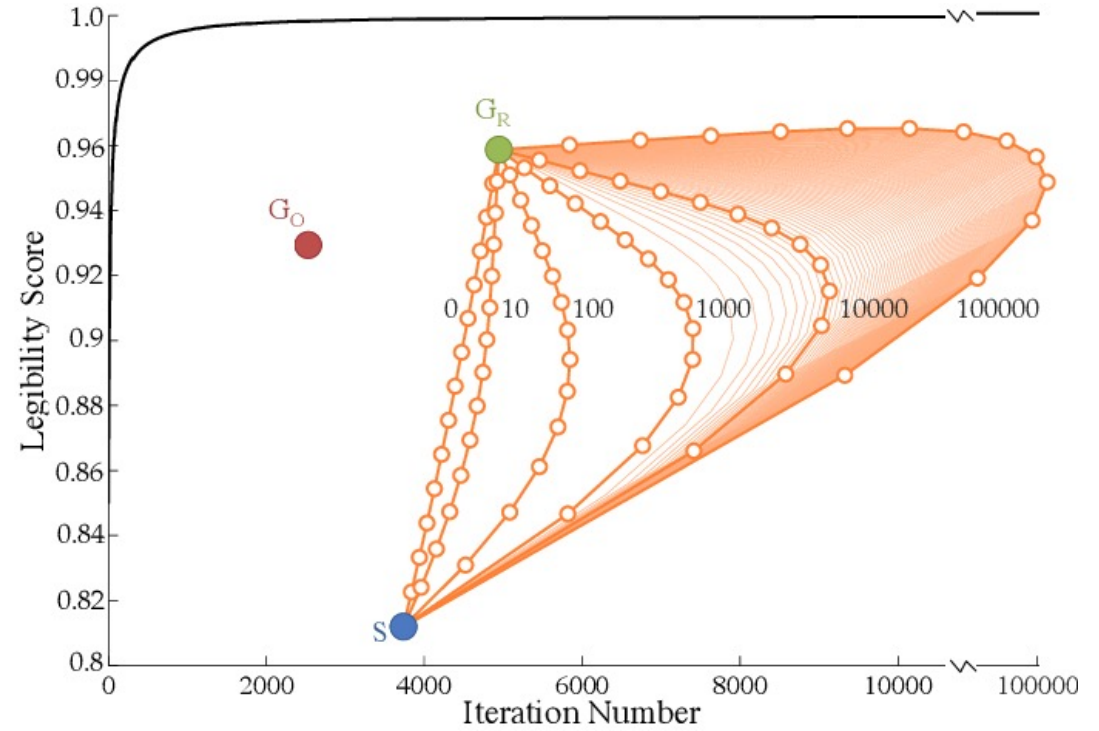


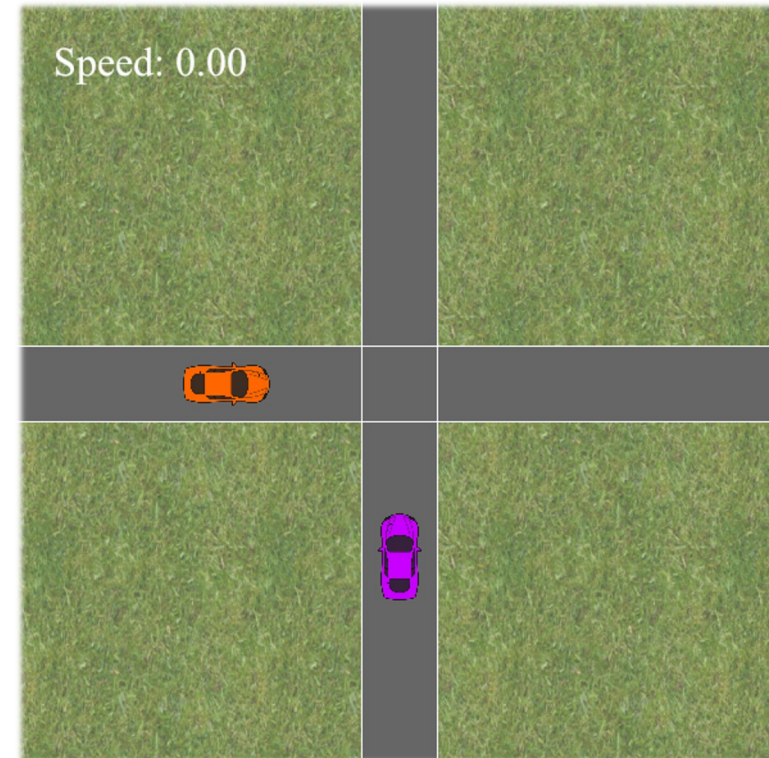
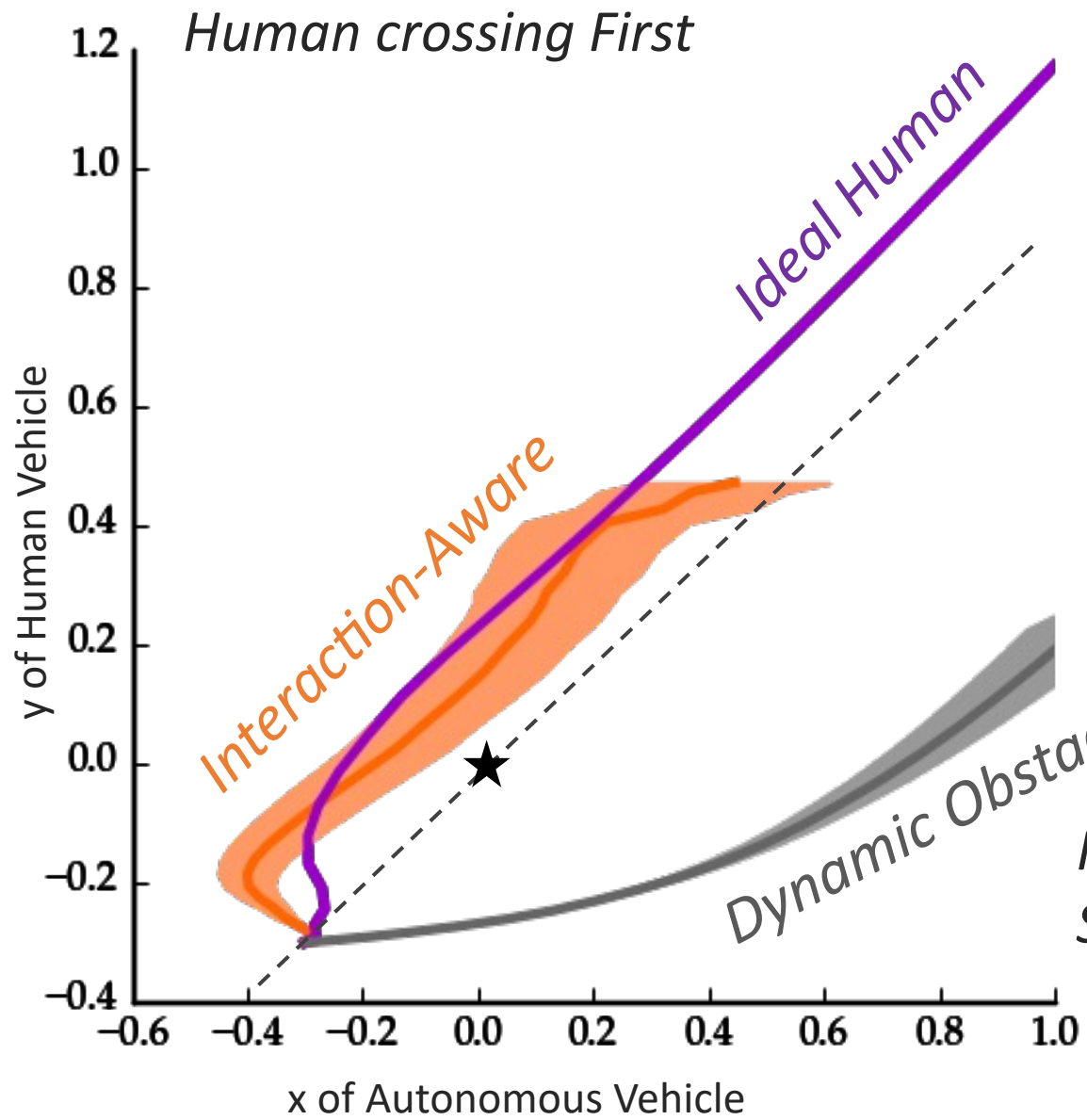
Implication: Coordination



Legible Motion

Using robot motion to coordinate with the human better about the robot's goal





Human crossing Second



$$p(u_{\mathcal{H}}|x) \propto \exp(R_{\mathcal{H}}(x, u_{\mathcal{H}}))$$





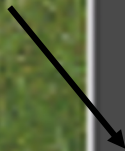
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We can't rely on a
single driver model.

We need to *differentiate*
between different drivers.



$$p(u_{\mathcal{H}} | x, \theta) \propto \exp(R_{\mathcal{H}}(x, u_{\mathcal{H}}, \theta))$$



$$b_{t+1}(\theta) \propto b_t(\theta) \cdot p(u_{\mathcal{H}} | x_t, \theta)$$



$$p(u_{\mathcal{H}} | x, \theta) \propto \exp(R_{\mathcal{H}}(x, u_{\mathcal{H}}, \theta))$$



$$b_{t+1}(\theta) \propto b_t(\theta) \cdot p(u_{\mathcal{H}} | x_t, \theta)$$

$$u_{\mathcal{R}} = \operatorname{argmax}_{u_{\mathcal{R}}} R_{\mathcal{R}}$$



Drivers *respond* to
actions of other cars.

...We have an opportunity to
actively gather information.



$$p(u_{\mathcal{H}}|x, \theta, u_{\mathcal{R}}) \propto \exp(R_{\mathcal{H}}(x, u_{\mathcal{H}}, \theta, u_{\mathcal{R}}))$$



$$b_{t+1}(\theta) \propto b_t(\theta) \cdot p(u_{\mathcal{H}}|x_t, \theta, u_{\mathcal{R}})$$

Info Gathering

$$R_{\mathcal{R}}(x, u_{\mathcal{H}}, \theta, u_{\mathcal{R}}) = \underbrace{\mathbb{H}(b_t) - \mathbb{H}(b_{t+1})}_{\text{Info Gathering}} + \underbrace{\lambda \cdot R_{goal}(x, u_{\mathcal{H}}, \theta, u_{\mathcal{R}})}_{\text{Goal}}$$

Goal



$$p(u_{\mathcal{H}}|x, \theta, u_{\mathcal{R}}) \propto \exp(R_{\mathcal{H}}(x, u_{\mathcal{H}}, \theta, u_{\mathcal{R}}))$$



$$b_{t+1}(\theta) \propto b_t(\theta) \cdot p(u_{\mathcal{H}}|x_t, \theta, u_{\mathcal{R}})$$

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$$R_{\mathcal{R}}(x, u_{\mathcal{H}}, \theta, u_{\mathcal{R}}) = \underbrace{\mathbb{H}(b_t) - \mathbb{H}(b_{t+1})}_{\text{Info Gathering}} + \underbrace{\lambda \cdot R_{goal}(x, u_{\mathcal{H}}, \theta, u_{\mathcal{R}})}_{\text{Goal}}$$

Goal

$$u_{\mathcal{R}} = \operatorname{argmax}_{u_{\mathcal{R}}} \mathbb{E}_{\theta} [R_{\mathcal{R}}]$$





$$p(u_{\mathcal{H}}|x, \theta, u_{\mathcal{R}}) \propto \exp(R_{\mathcal{H}}(x, u_{\mathcal{H}}, \theta, u_{\mathcal{R}}))$$



$$b_{t+1}(\theta) \propto b_t(\theta) \cdot p(u_{\mathcal{H}}|x_t, \theta, u_{\mathcal{R}})$$

Info Gathering

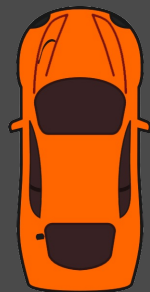
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Goal

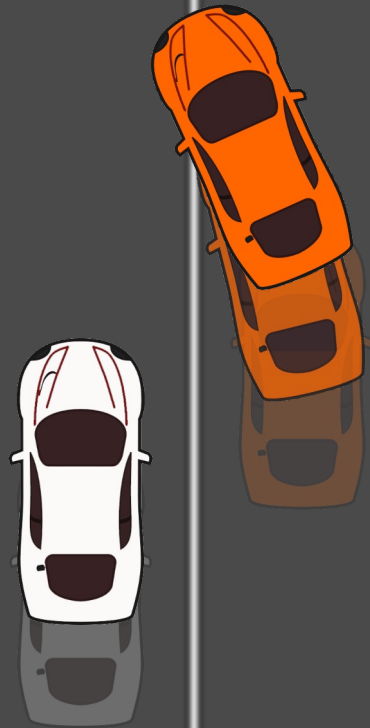
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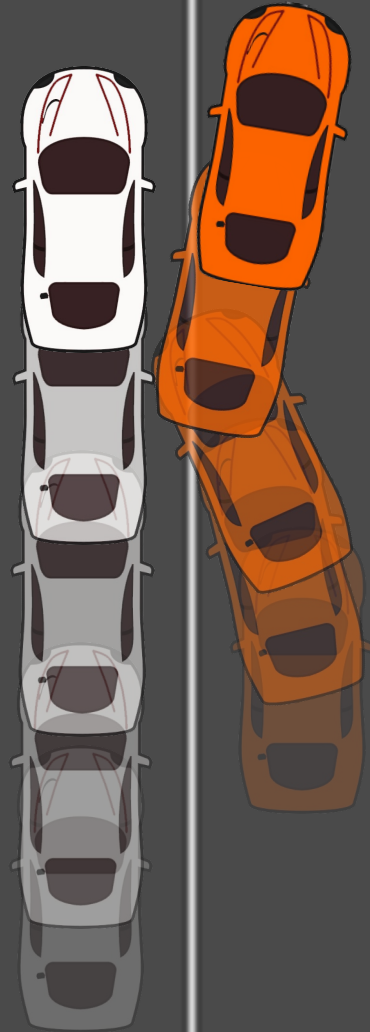
Nudging in for Active Info Gathering



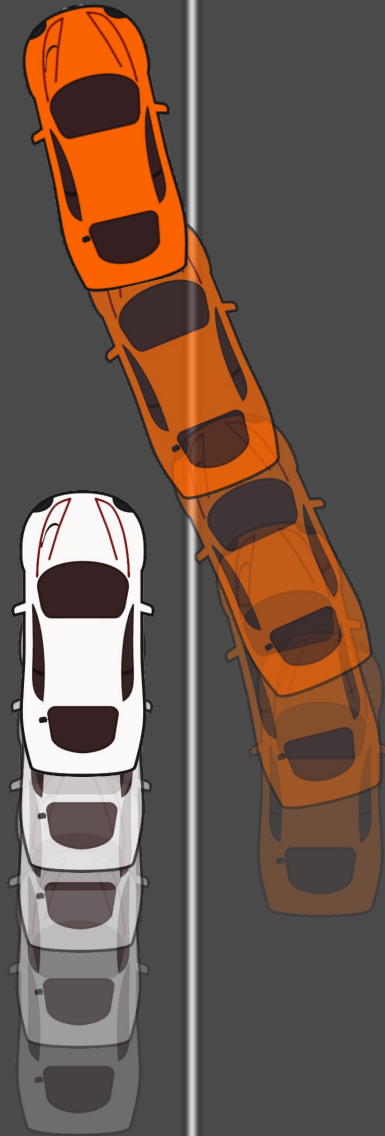
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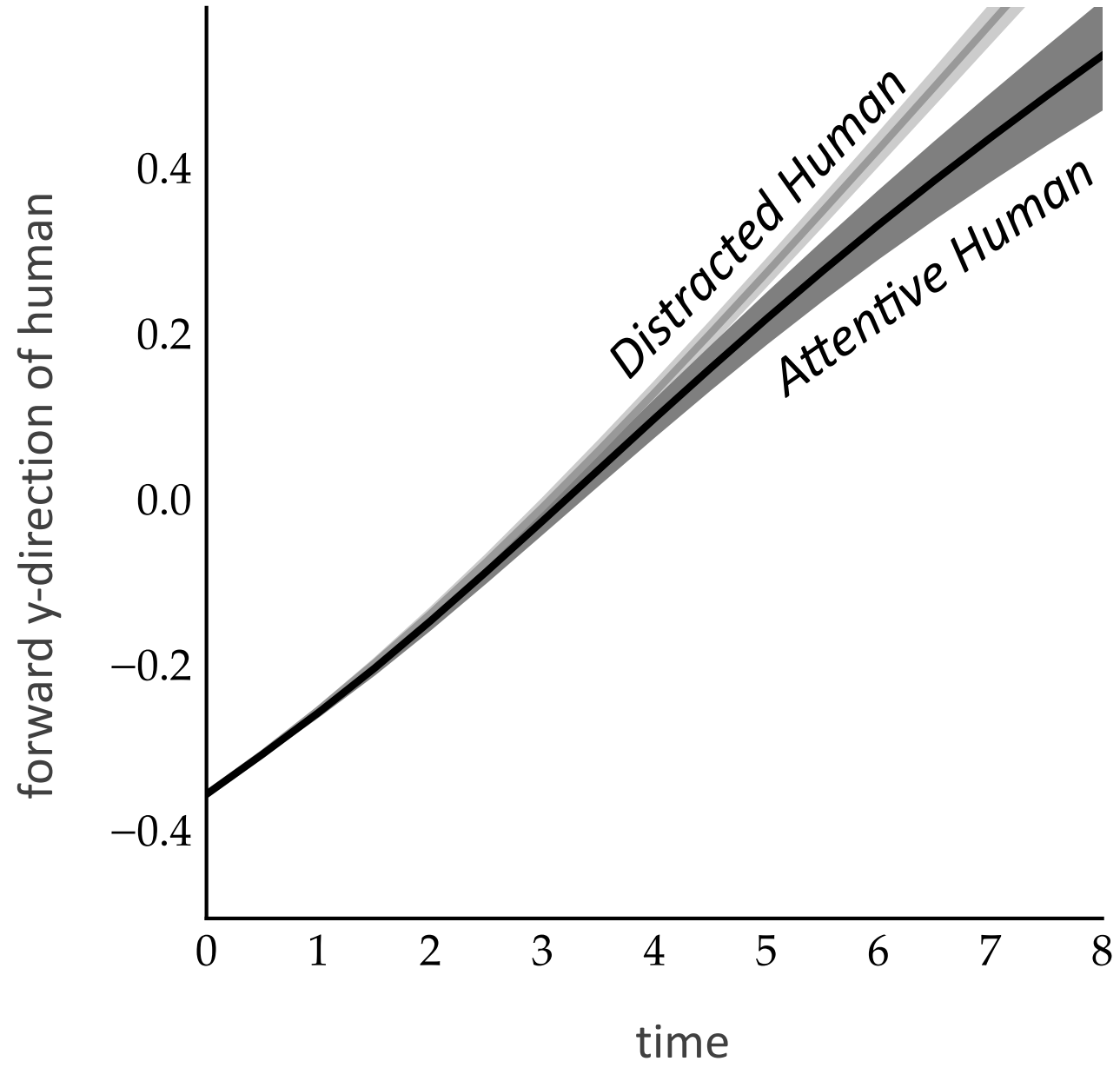


Distracted Human

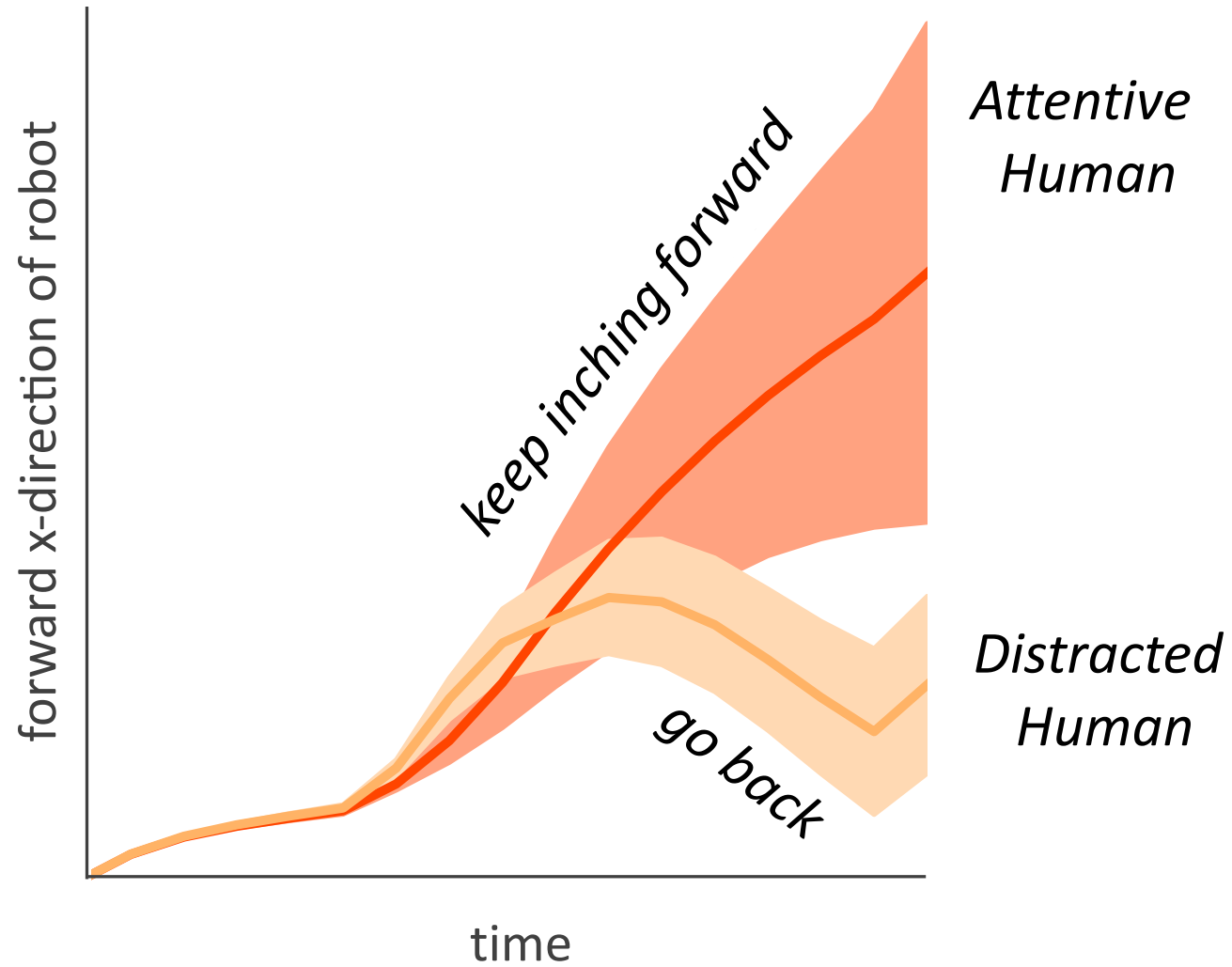


Attentive Human

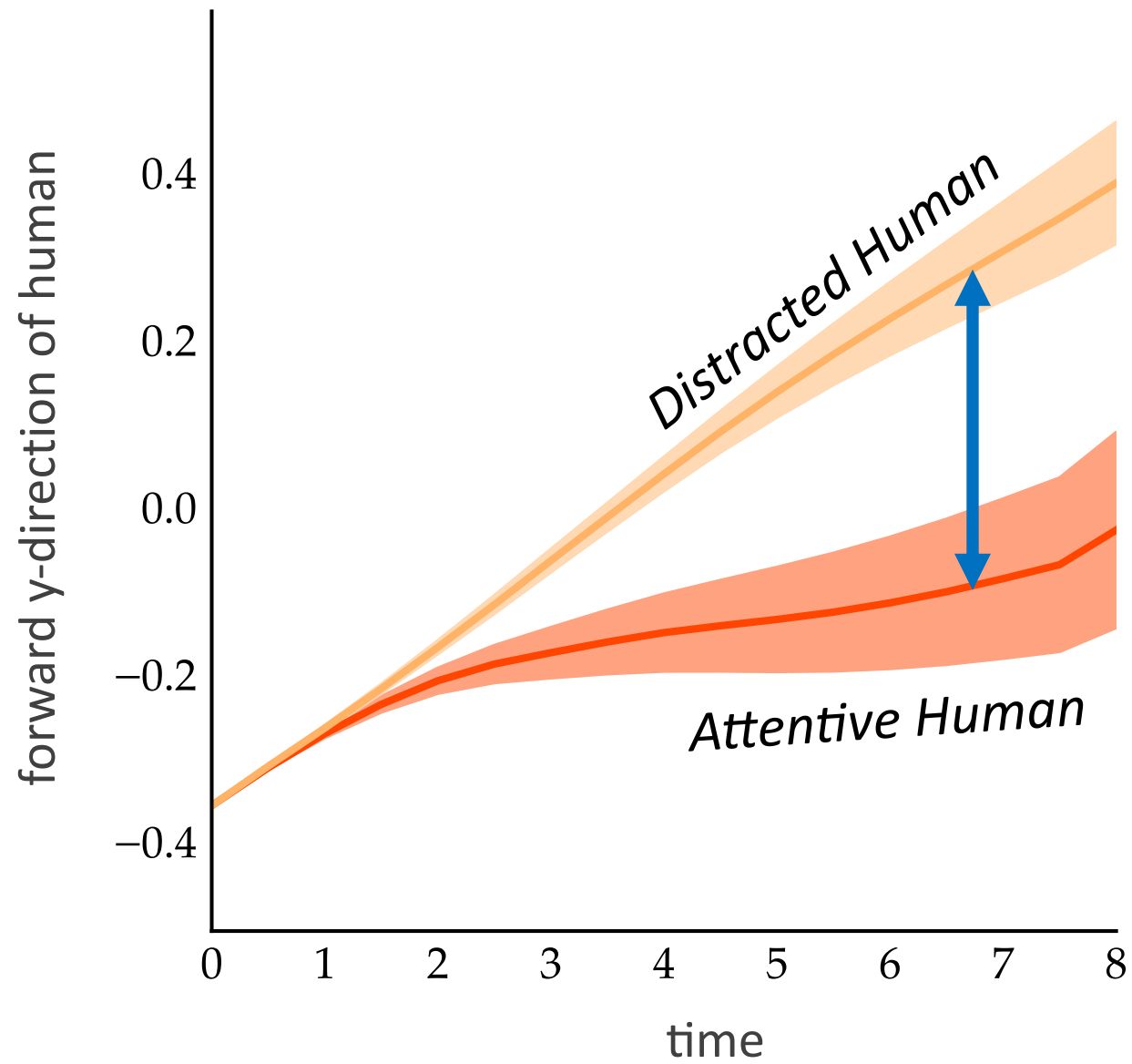




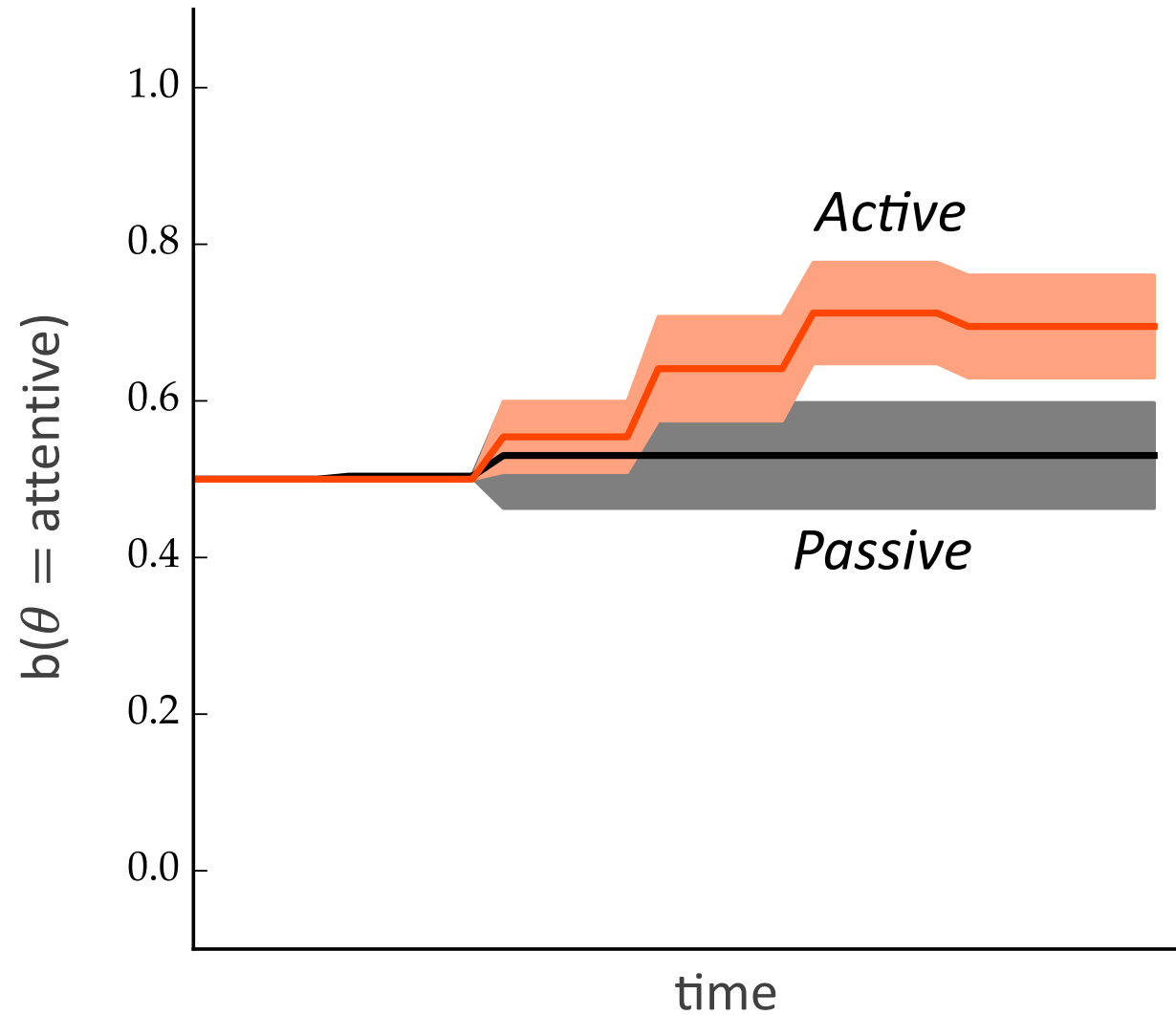
Robot Active Info Gathering



Human Responses



Belief over Driving Style: Active vs Passive



Key Idea:

Robot's actions *affect* human's actions. We want to *leverage* these effects for better safety and efficiency and better estimation.

Today's itinerary

- Game-Theoretic Views on Multi-Agent Interactions
- Partner Modeling: Active Info Gathering over Human's Intent
- Partner Modeling: Learning and Influencing Latent Intent
- Partner Modeling: Role Assignment