

Principles of Robot Autonomy II

Human-Robot Interaction



Stanford
University



Announcement

Paper presentation for 4-credit students due next Wednesday.

Turn them in on Gradescope (slides for live presenters, video recordings for non-live presenters)

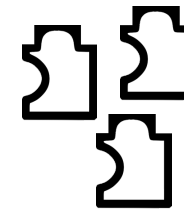
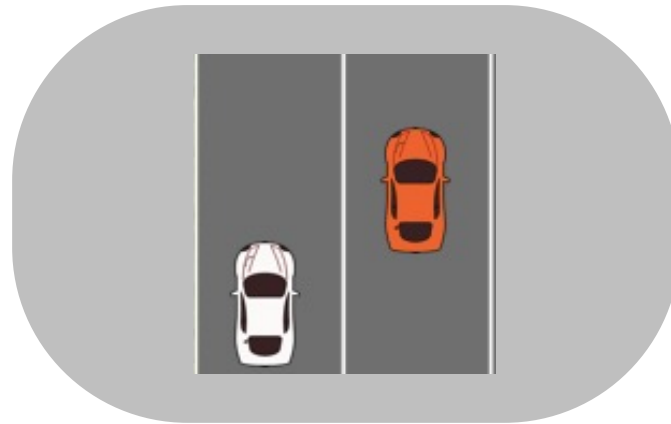
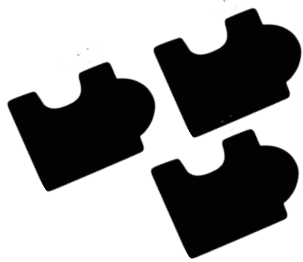
Today's itinerary

- Game-Theoretic Views on Multi-Agent Interactions
- Partner Modeling: Active Info Gathering over Human's Intent
- Partner Modeling: Learning and Influencing Latent Intent
- Partner Modeling: Role Assignment

Today's itinerary

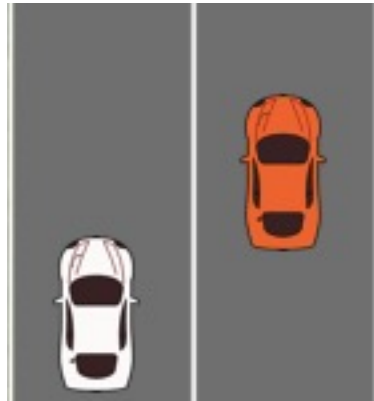
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Nth order Theory of Mind



Interaction as a Dynamical System

$$u_{\mathcal{R}}^* = \operatorname{argmax}_{u_{\mathcal{R}}} R_{\mathcal{R}}(x, u_{\mathcal{R}}, u_{\mathcal{H}}^*(x, u_{\mathcal{R}}))$$



Find optimal actions for the robot while accounting for the human response $u_{\mathcal{H}}^*$.

Model $u_{\mathcal{H}}^*$ as optimizing the human reward function $R_{\mathcal{H}}$.

$$u_{\mathcal{H}}^*(x, u_{\mathcal{R}}) \approx \operatorname{argmax}_{u_{\mathcal{H}}} R_{\mathcal{H}}(x, u_{\mathcal{R}}, u_{\mathcal{H}})$$



$$p(u_{\mathcal{H}}|x, \theta, u_{\mathcal{R}}) \propto \exp(R_{\mathcal{H}}(x, u_{\mathcal{H}}, \theta, u_{\mathcal{R}}))$$



$$b_{t+1}(\theta) \propto b_t(\theta) \cdot p(u_{\mathcal{H}}|x_t, \theta, u_{\mathcal{R}})$$

Info Gathering

$$R_{\mathcal{R}}(x, u_{\mathcal{H}}, \theta, u_{\mathcal{R}}) = \underbrace{\mathbb{H}(b_t) - \mathbb{H}(b_{t+1})}_{\text{Info Gathering}} + \underbrace{\lambda \cdot R_{goal}(x, u_{\mathcal{H}}, \theta, u_{\mathcal{R}})}_{\text{Goal}}$$

Goal

$$u_{\mathcal{R}} = \operatorname{argmax}_{u_{\mathcal{R}}} \mathbb{E}_{\theta} [R_{\mathcal{R}}]$$



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Info Gathering

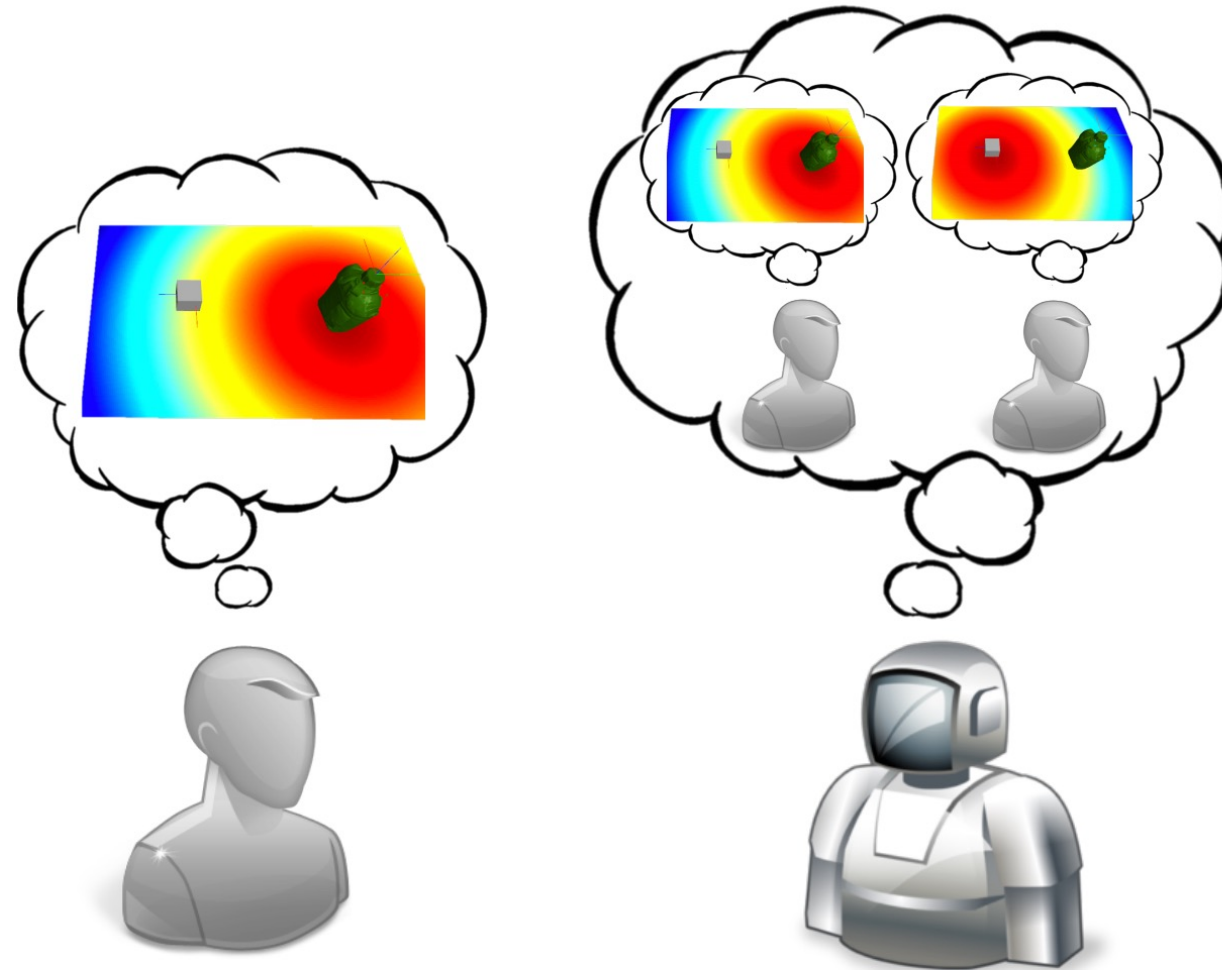
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Goal

$$u_{\mathcal{R}} = \operatorname{argmax}_{u_{\mathcal{R}}} \mathbb{E}_{\theta} [R_{\mathcal{R}}]$$



Modeling Intent Inference using POMDPs



POMDP Formulation

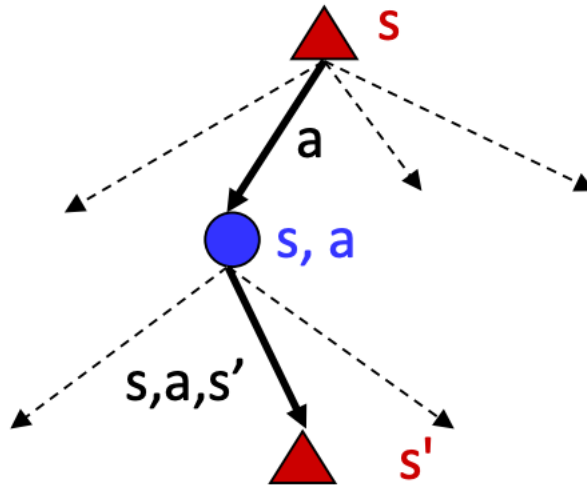
MDPs have:

States S

Actions A

Transition Function $P(s'|s, a)$

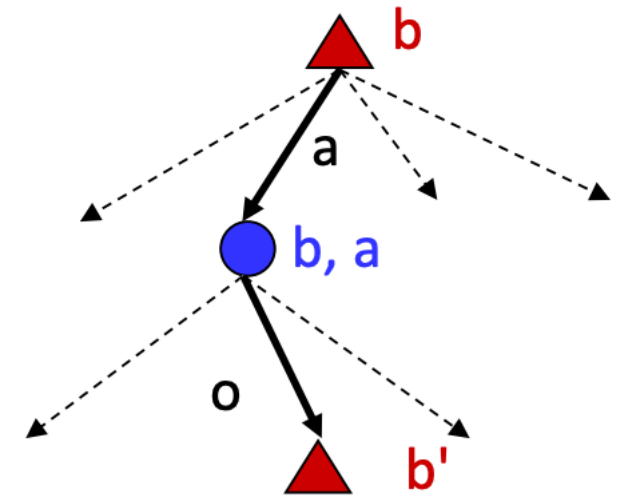
Reward $R(s, a, s')$



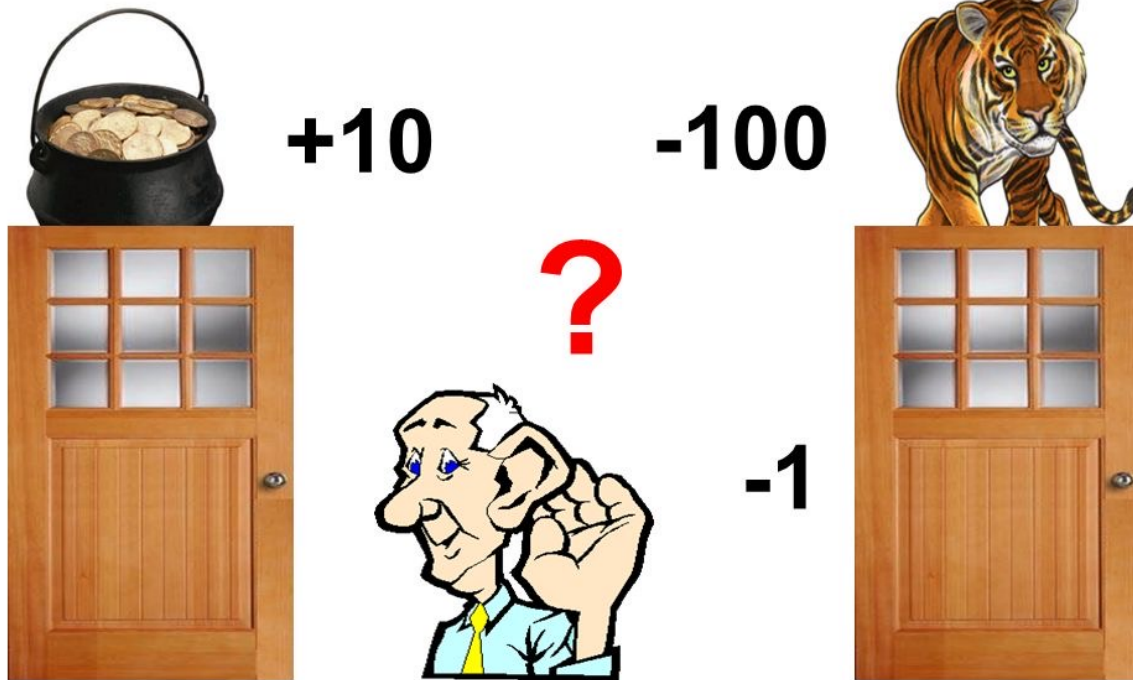
POMDPs add:

Observations O

Observation Function $P(o|s)$



Tiger Example



Actions $a = \{0, 1, 2\}$: 0: listen, 1: open left, 2: open right

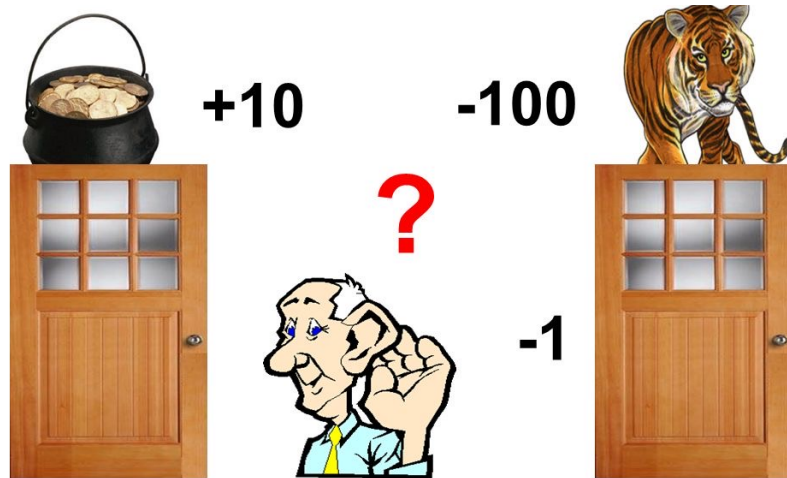
Reward Function:

- Penalty for wrong opening: -100
- Reward for correct opening: +10
- Cost of listening: -1

Observations:

- To hear the tiger on the left
- To hear the tiger on the right

Tiger Example



Belief update based on observations:

$$b_1(s_i) \propto p(o|s_i, a) \sum_{s_j \in \mathcal{S}} p(s_i|s_j, a) \cdot b_0(s_j)$$

Immediate return

Discounted future return

Value Iteration
over Beliefs

$$V^*(b) = \max_{a \in A} \left[\sum_{s \in \mathcal{S}} b(s) \cdot R(s, a) + \gamma \sum_{o \in \mathcal{O}} P(o|b, a) \cdot V^*(b_o^a) \right]$$

Hard to compute continuous space MDPs -> Approximation

Tiger Example

Value Iteration
over Beliefs

$$V^*(b) = \max_{a \in A} \left[\sum_{s \in S} b(s) \cdot R(s, a) + \gamma \sum_{o \in O} P(o|b, a) \cdot V^*(b_o^a) \right]$$

Immediate return *Discounted future return*

Hard to compute continuous space MDPs -> Approximation

Q-MDP
Approximation

$$V^*(b) = \mathbb{E}_s[V^*(s)] = \sum_s b(s) \cdot V^*(s)$$

Intent Inference

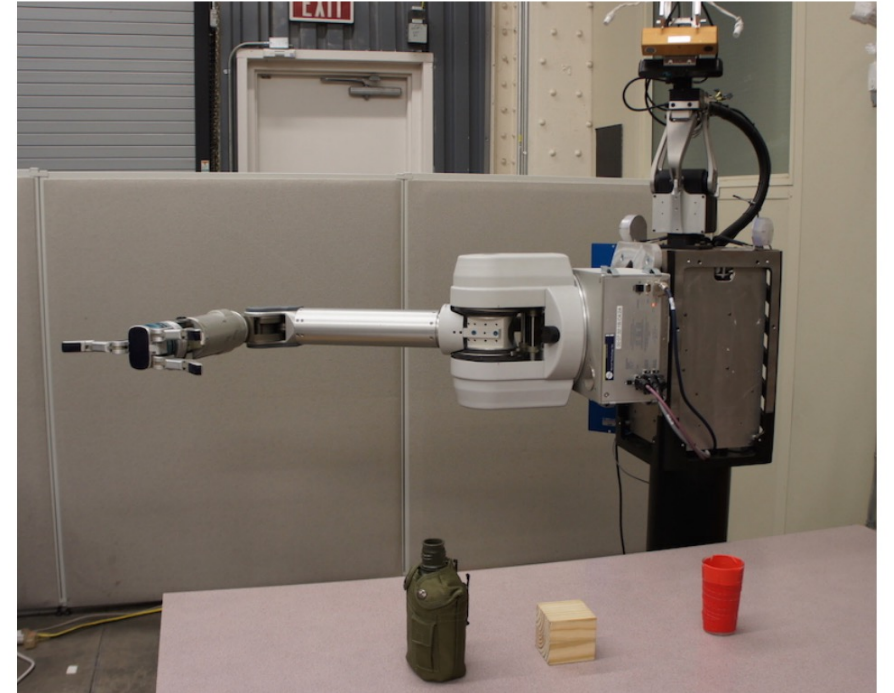
X Robot States

A Robot Actions

$T: X \times A \rightarrow X$ Transition function

$u \in U$ Human continuous input

$D: U \rightarrow A$ Mapping between human input and robot actions



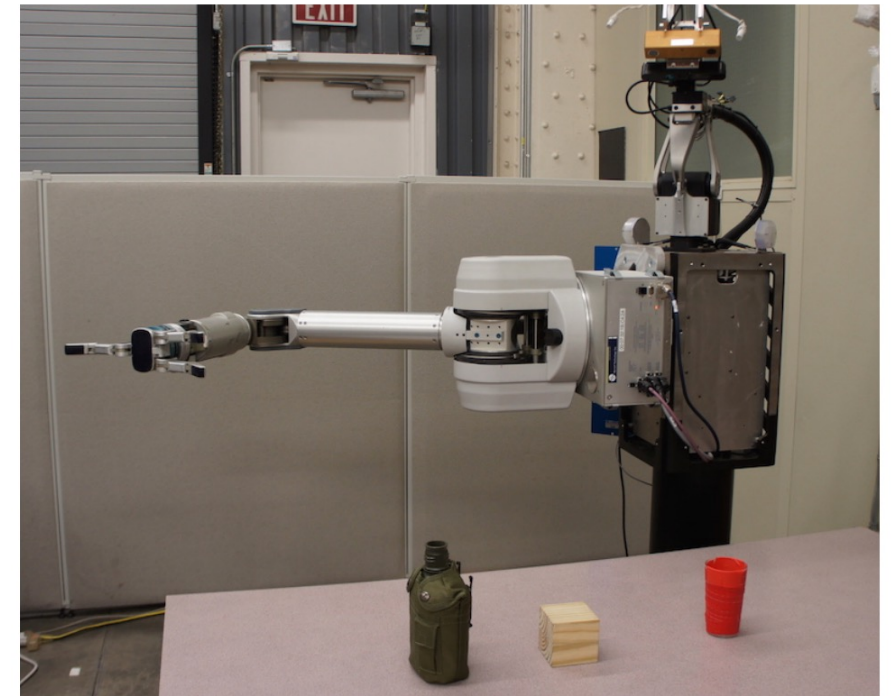
User's Policy is Learned from IRL

$\pi_g^{usr}(x) = p(u|x, g)$ We learn a policy for each goal

$$p(\xi|g) \propto \exp(-C_g^{usr}(\xi))$$

$$p(g|\xi) \propto p(\xi|g) \cdot p(g) \quad \text{Bayes Rule}$$

POMDP Observation Model



Hindsight Optimization (Q-MDP)

Estimate cost-to-go of the belief by assuming full observability will be obtained at the next time step.

You never gather information, but can plan efficiently in deterministic subproblems.

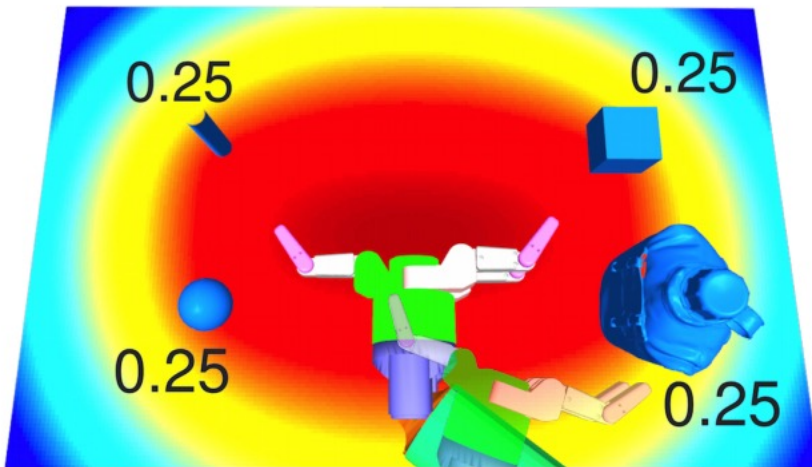
$$b(s) = b(g) = p(g|\xi) \quad \text{Uncertainty is only over goals}$$



$$Q(b, a, u) = \sum_g b(g) \cdot Q_g(x, a, u)$$

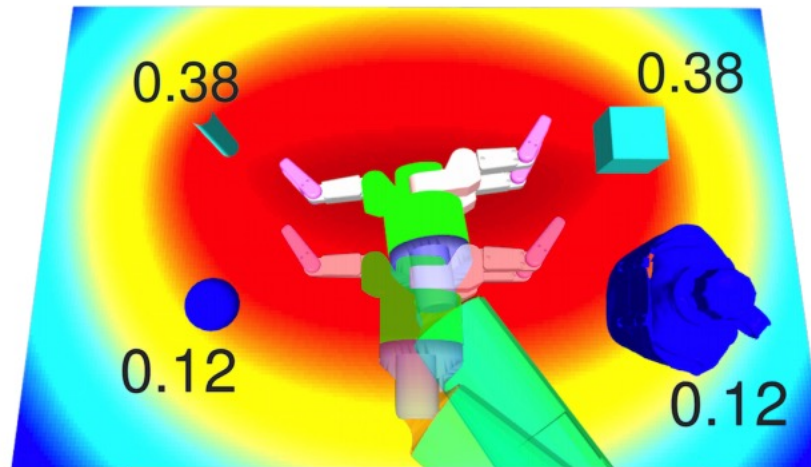
Action-Value function of the POMDP

Cost-to-Go of Acting optimally and going towards goal g

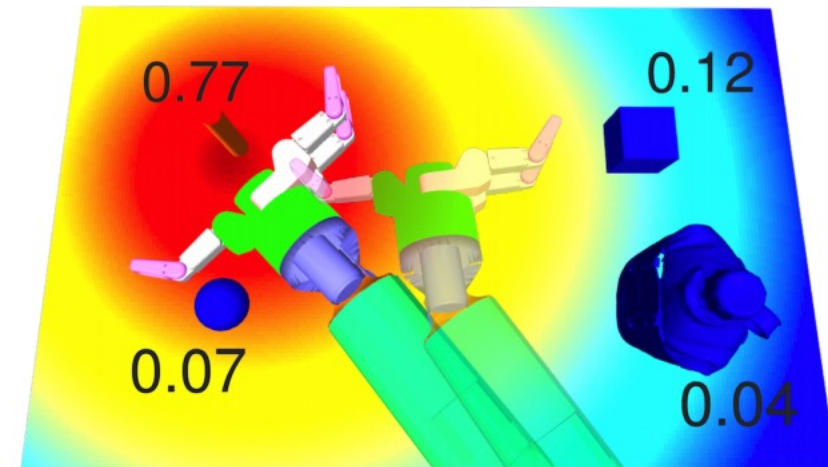
Shared Autonomy with Hindsight Optimization



User  Robot 



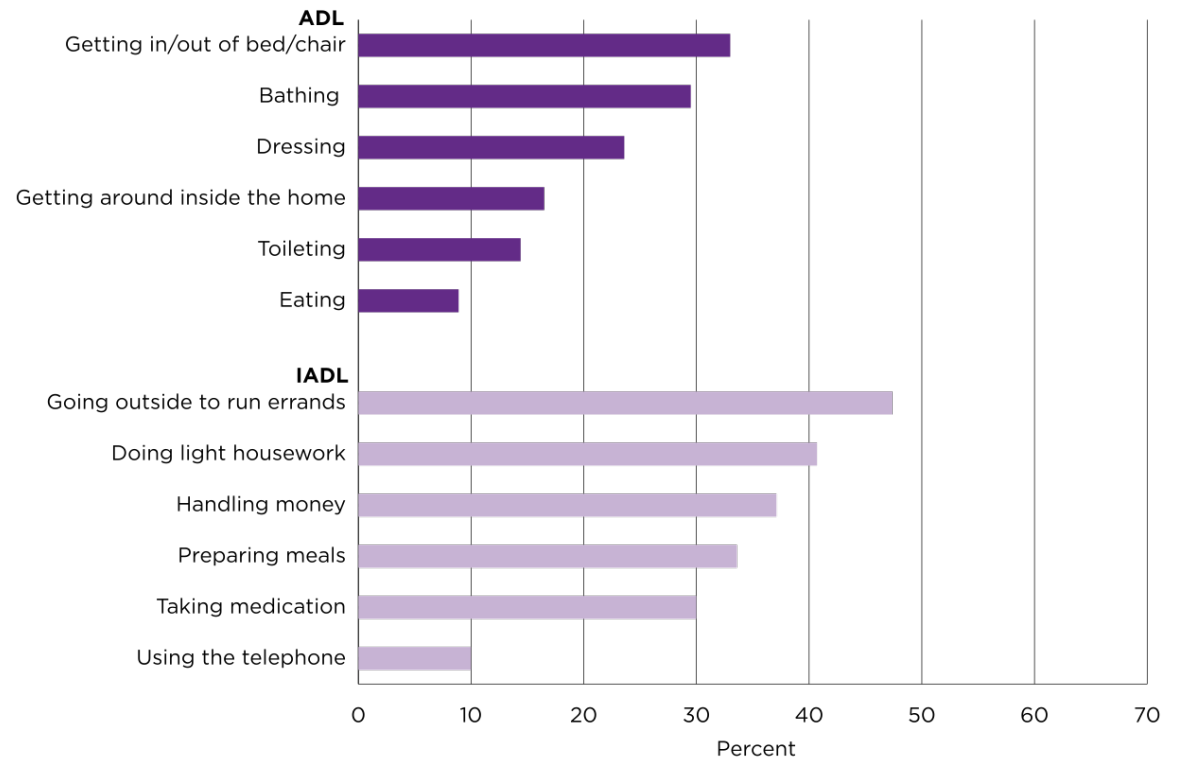
User  Robot 



User  Robot 

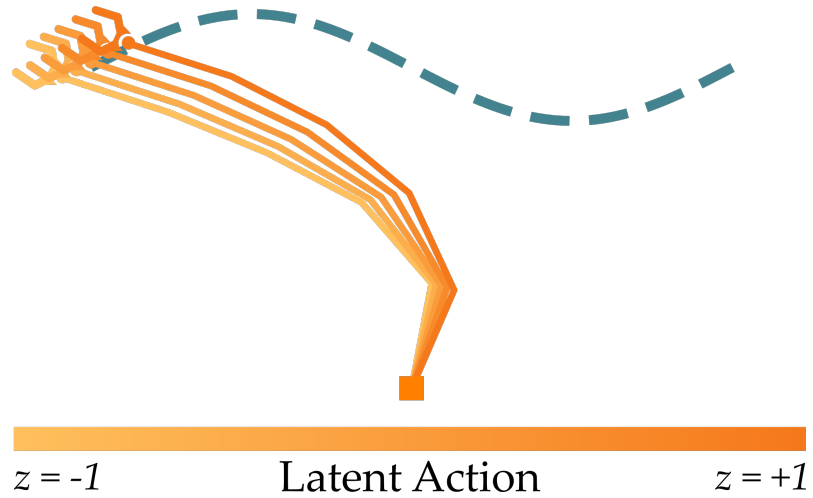


Prevalence of Difficulty Performing ADLs and IADLs in Adults 18 Years and Older With One or More Selected Symptoms That Interfere With Everyday Activities: 2014



Source: U.S. Census Bureau, Social Security Administration Supplement to the 2014 Panel of the Survey of Income and Program Participation, September–November 2014.





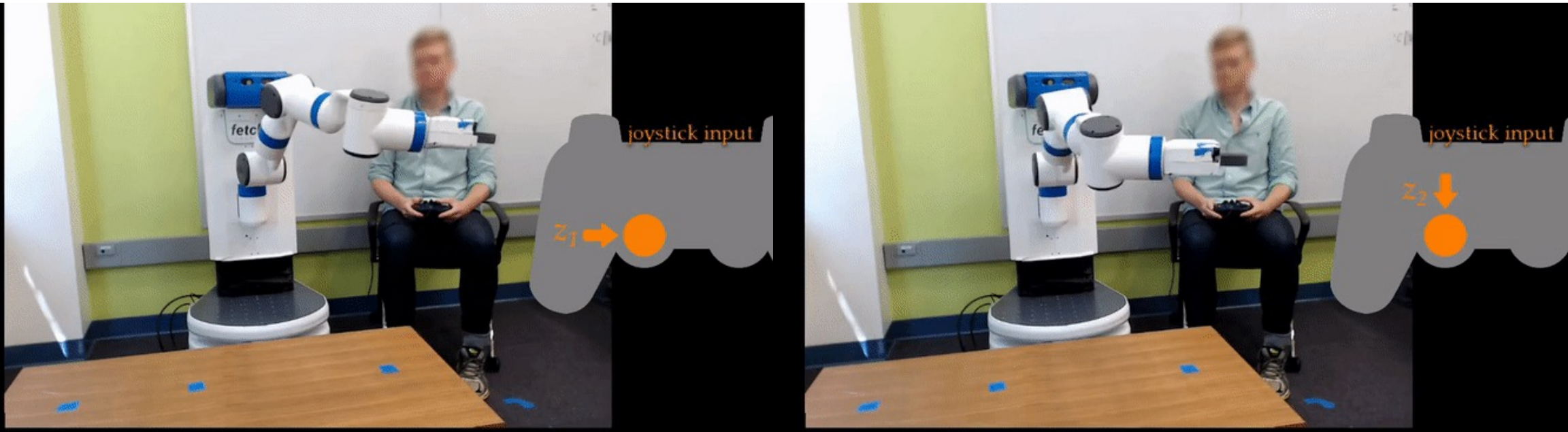
- Assistive robotic arms are *dexterous*
- This dexterity makes it hard for users to *control* the robot
- How can robots *learn* low-dimensional representations that make controlling the robot intuitive?

Our Vision



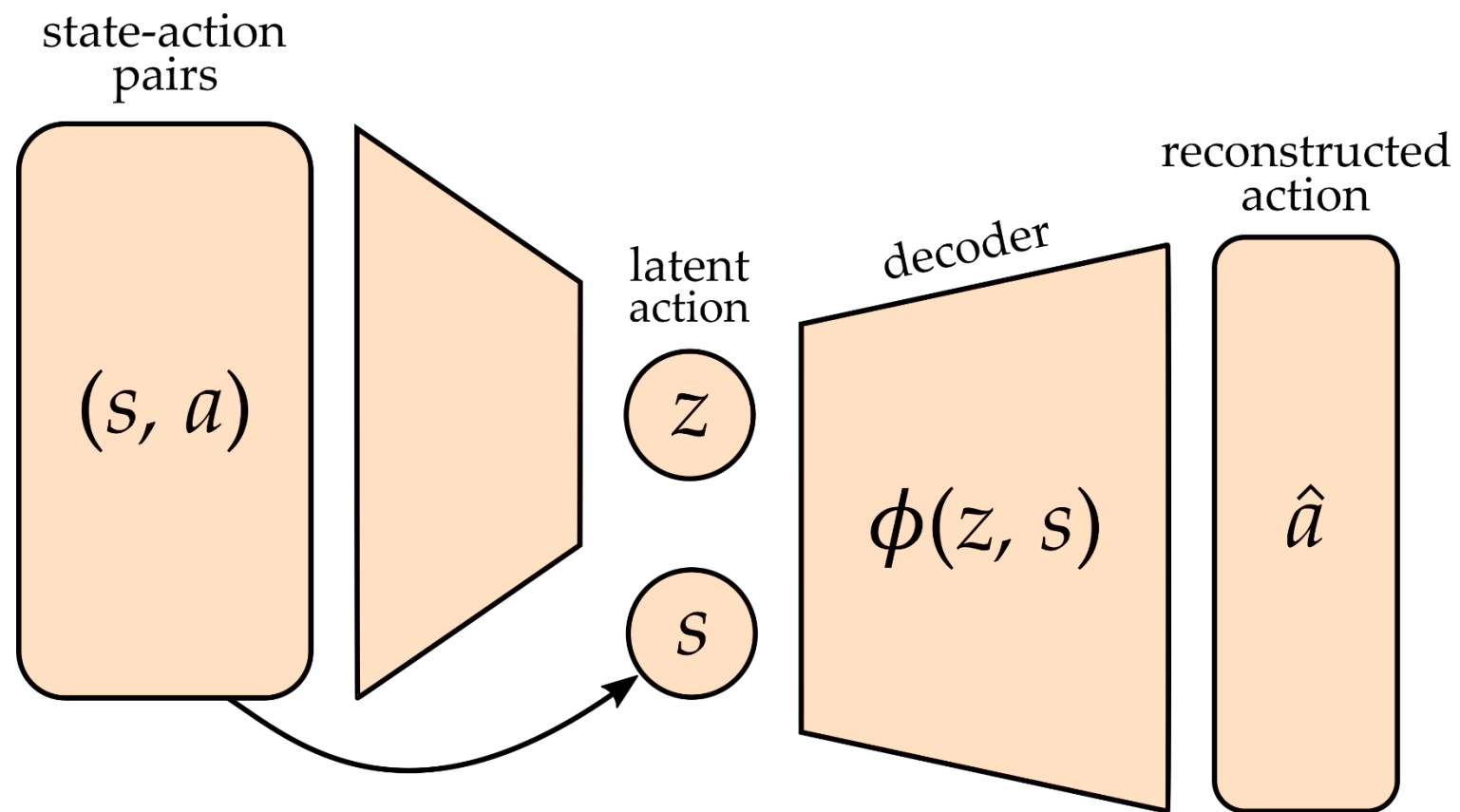
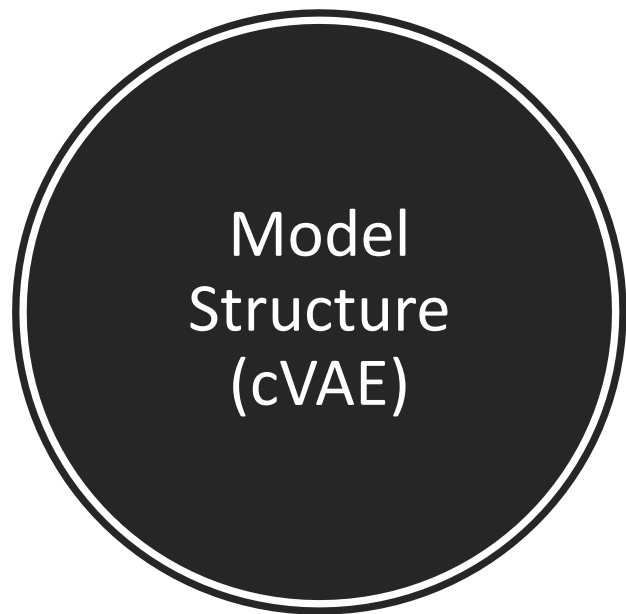
Offline, expert demonstrations of *high-dimensional* motions

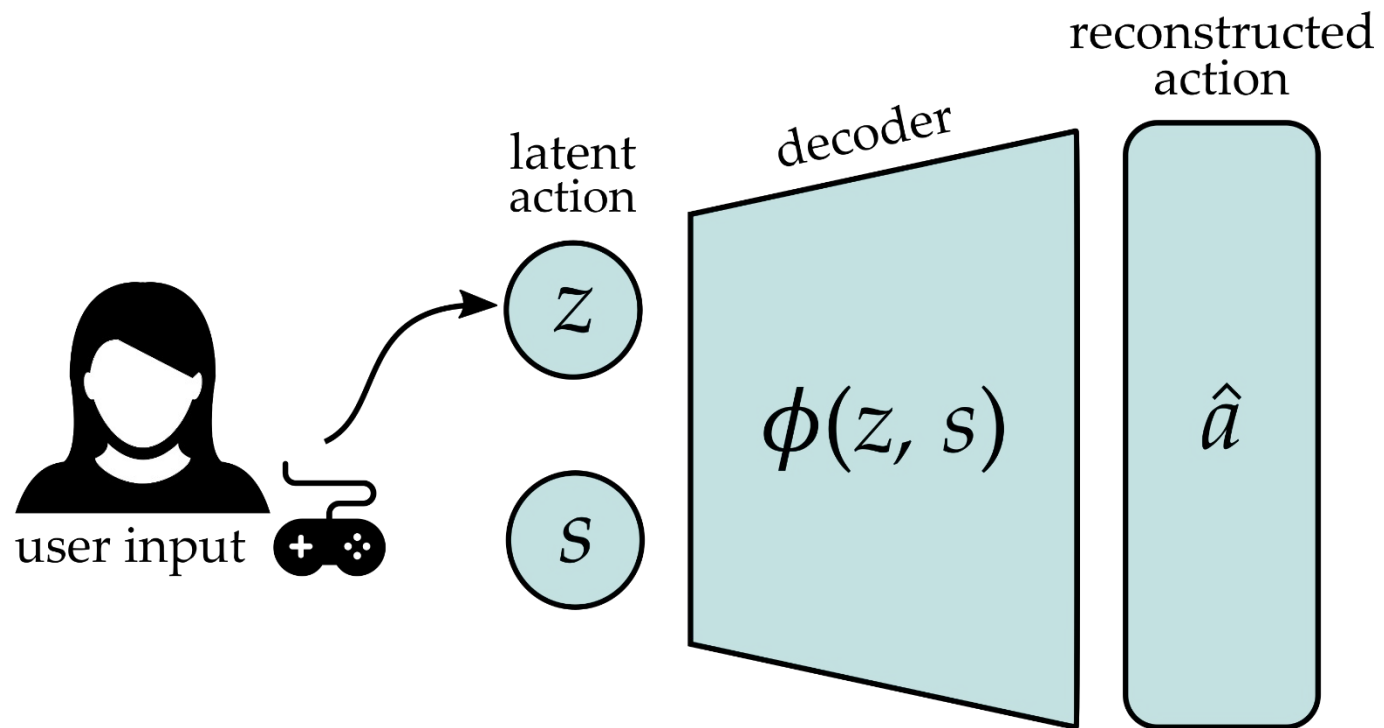
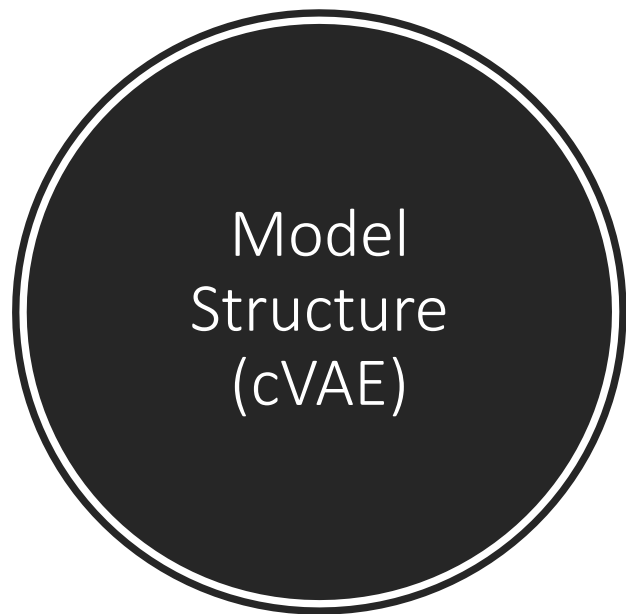
Our Vision



Learn *low-dimensional* latent representations for online control

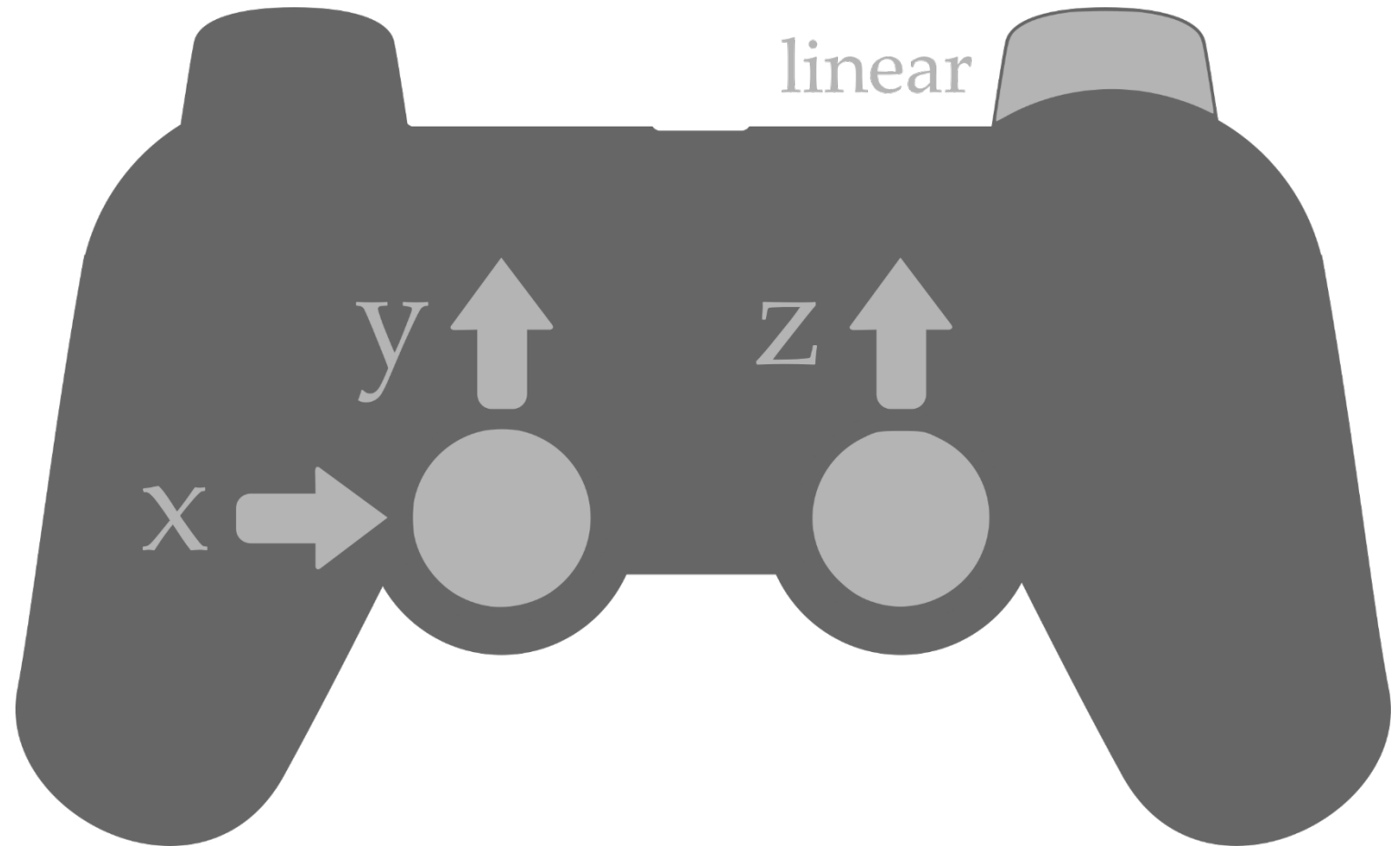
We make it easier to control *high-dimensional* robots by *embedding* the robot's actions into a *low-dimensional* latent space.

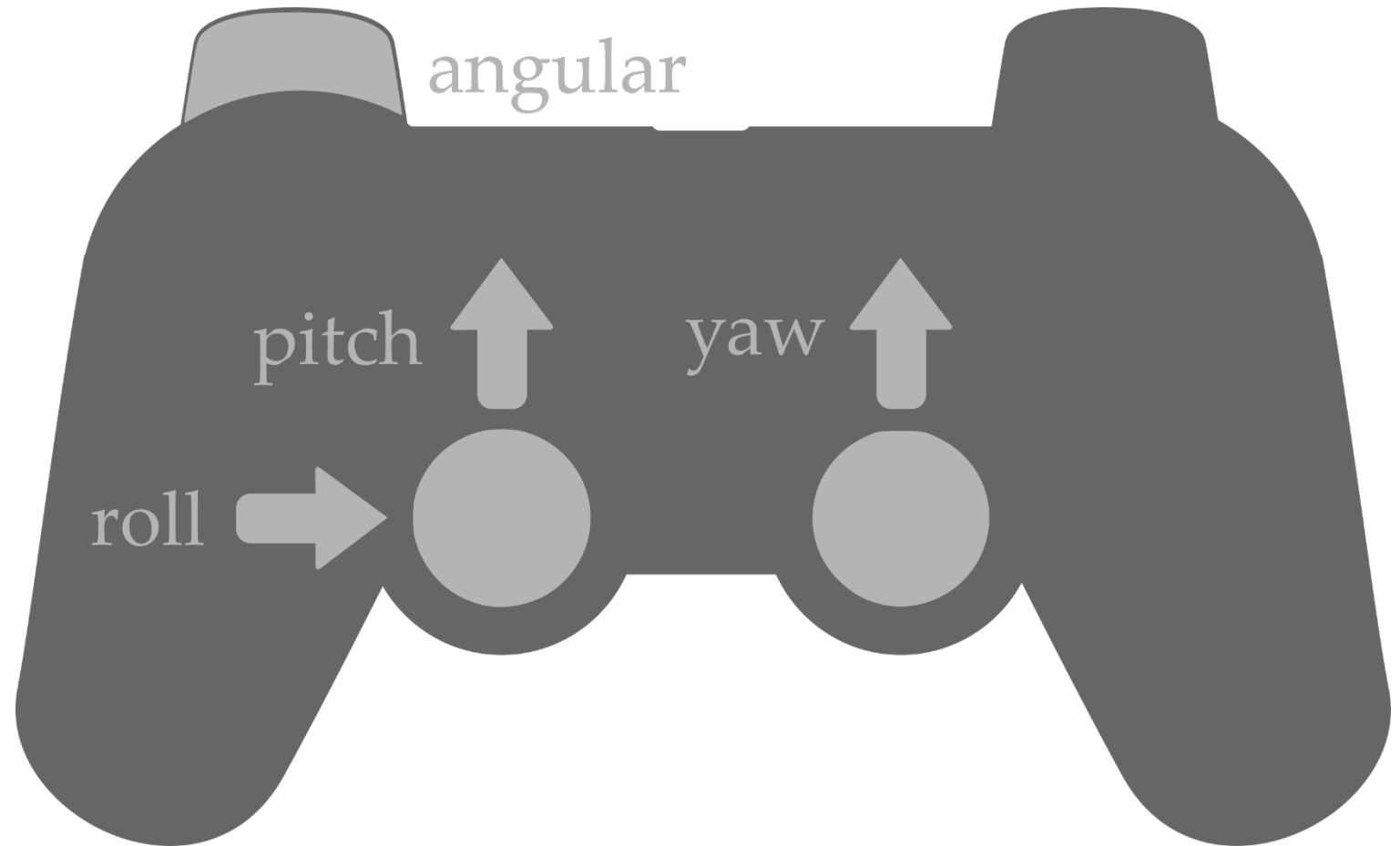


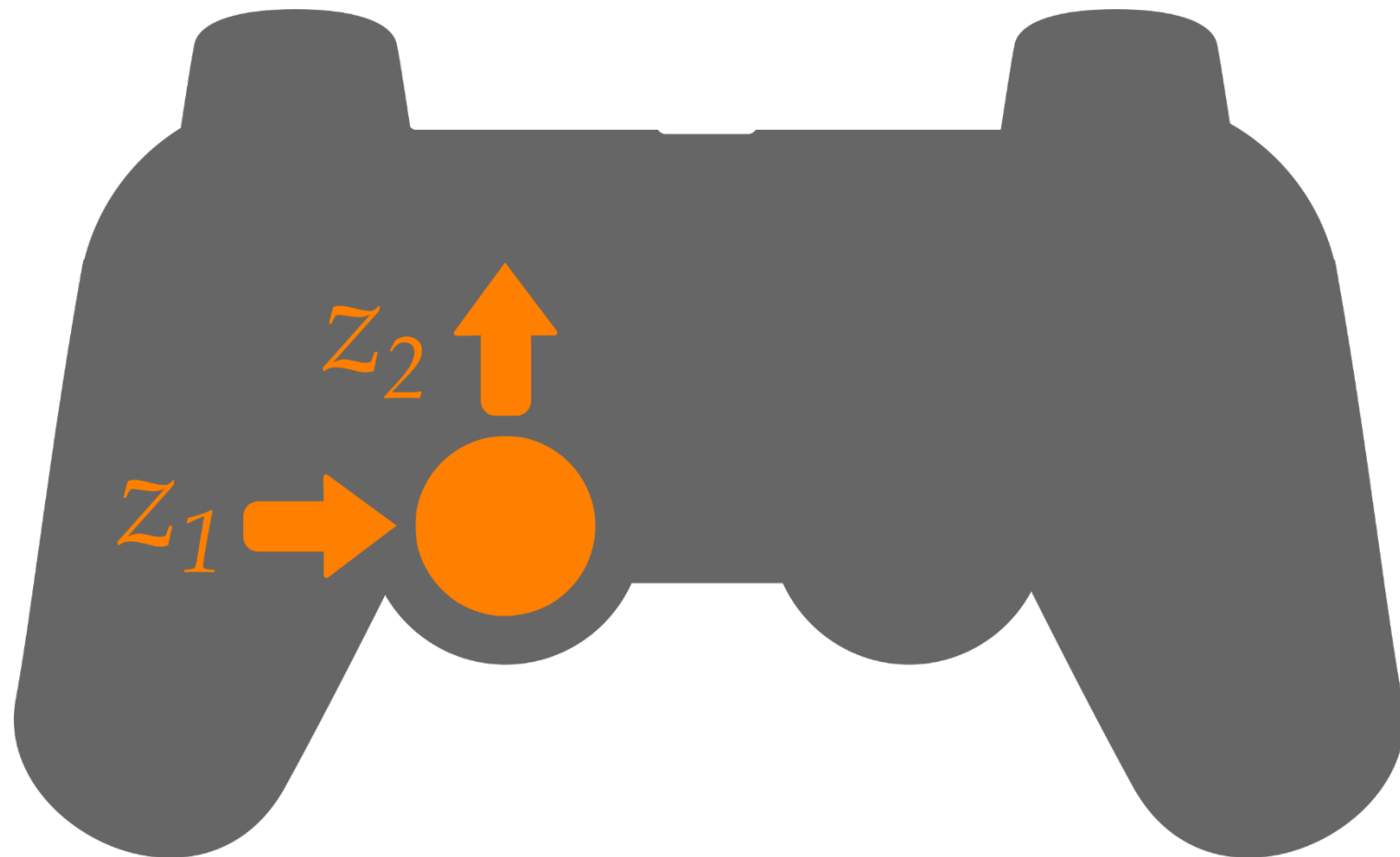


User Study

- We trained on less than **7 minutes** of kinesthetic demonstrations
- Demonstrations consisted of moving between shelves, pouring, stirring, and reaching motions
- We compared our **Latent Action** to the current method for assistive robotic arms (**End-Effector**)







4x Speed

(1) add eggs



End-Effector

(1) add eggs



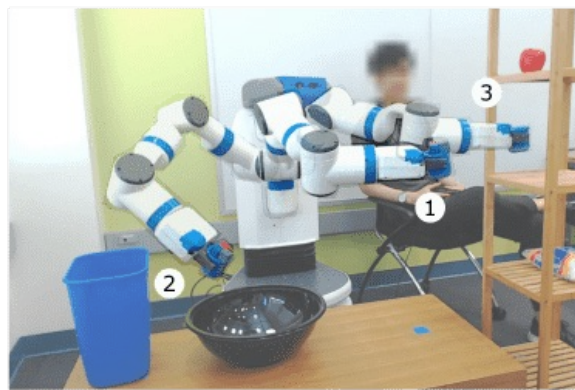
Latent Action

Add Eggs & Recycle

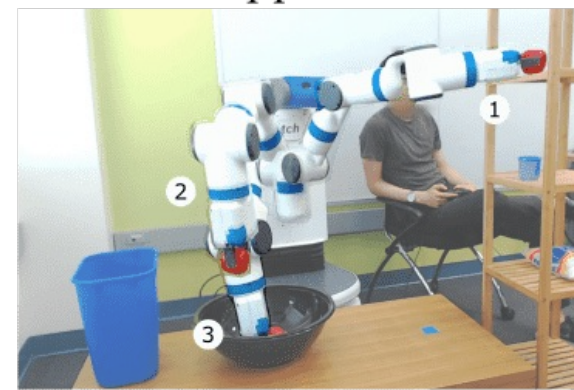
Task



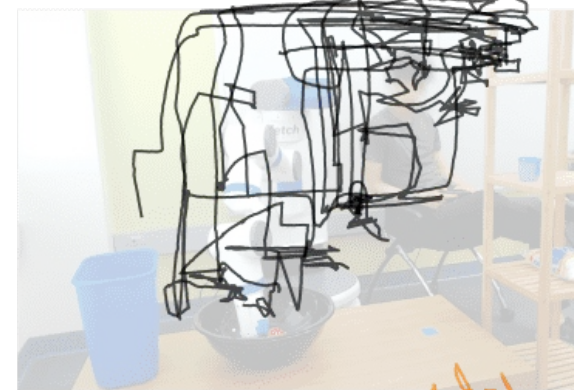
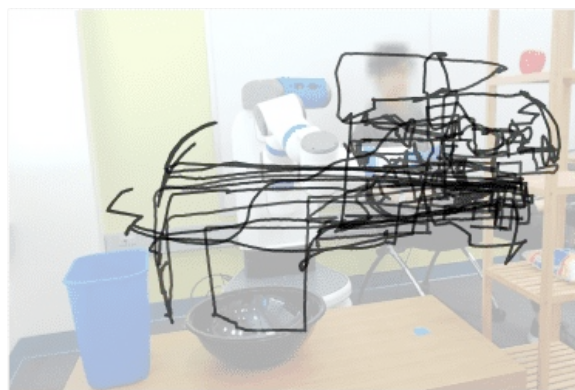
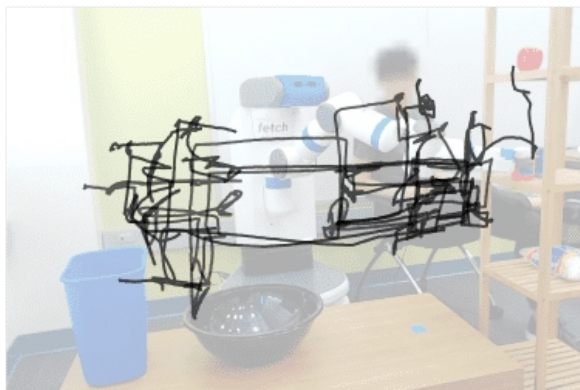
Add Flour & Return



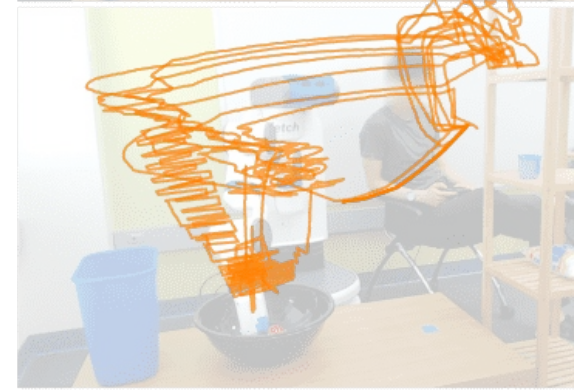
Add Apple and Stir



End-Effector



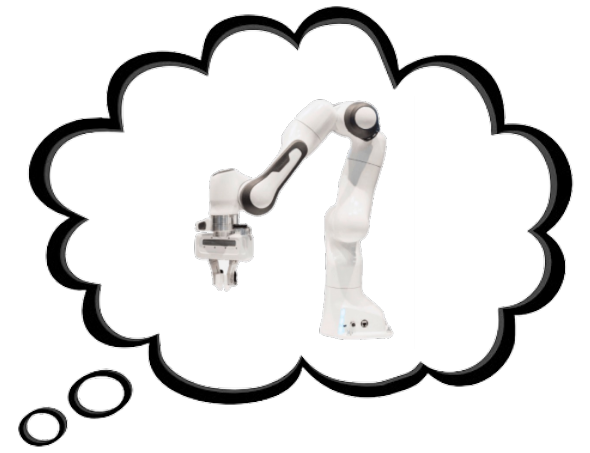
cVAE (ours)



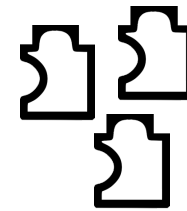
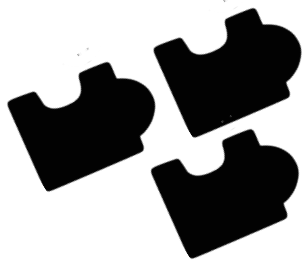
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Nth order Theory of Mind

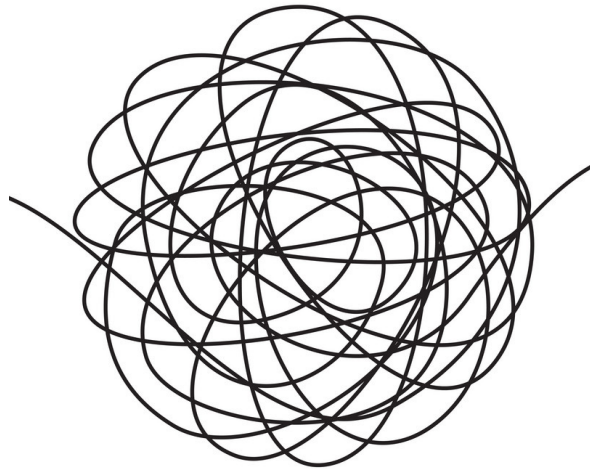


Most interactive tasks are not the same as playing chess!





... **low-dimensional** shared representation
that captures the interaction and can change over time.





Other agents are often **non-stationary**:
They update their behavior in response to the robot.

Ego Agent

Other Agent

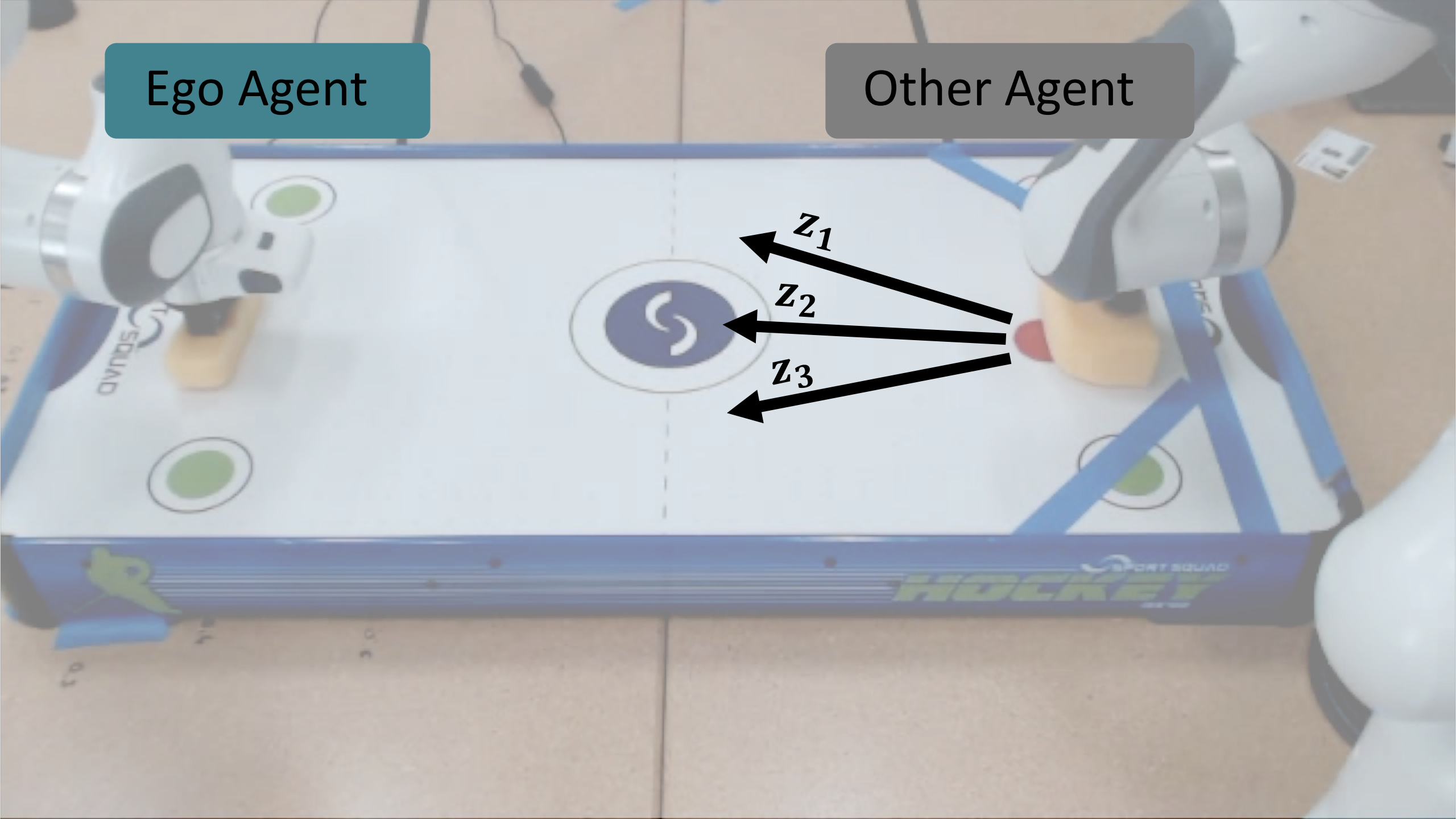


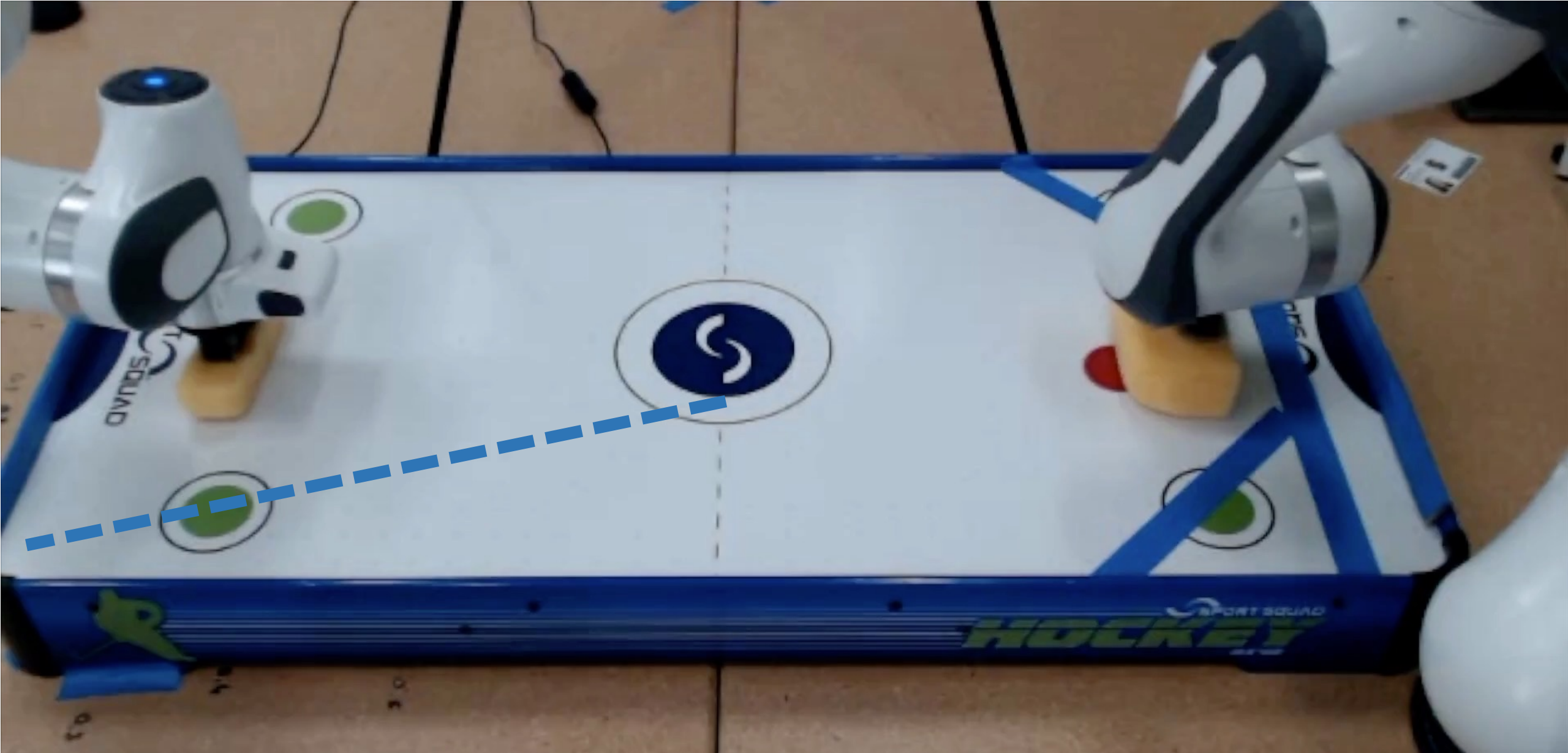
$$a \in \mathbb{R}^7$$



Ego Agent

Other Agent





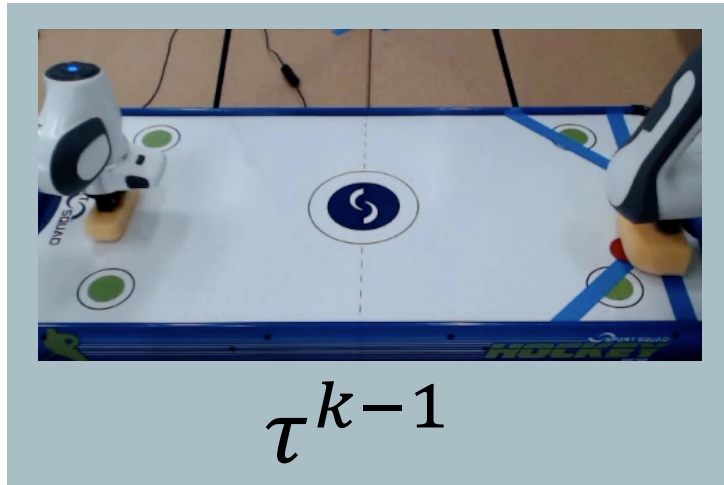
$$\tau^i = \{(s_1, a_1, r_1), \dots, (s_H, a_H, r_H)\}$$



$$z^{i+1} \sim f(\cdot | z^i, \tau^i)$$

Modeling Other Agent's Behavior

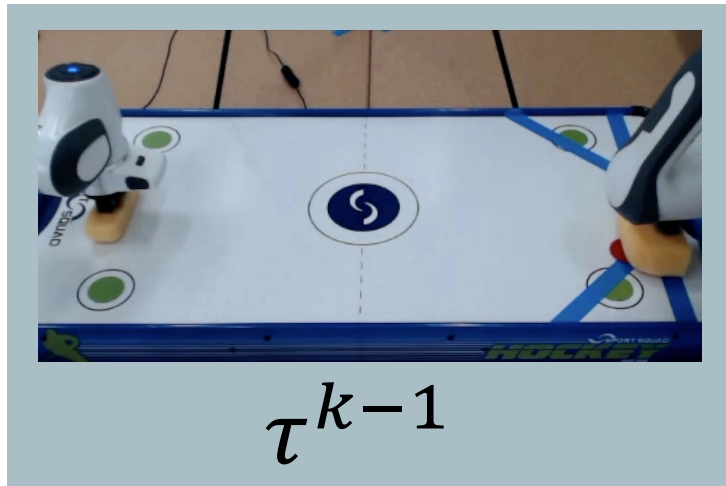
Modeling Other Agent's Behavior



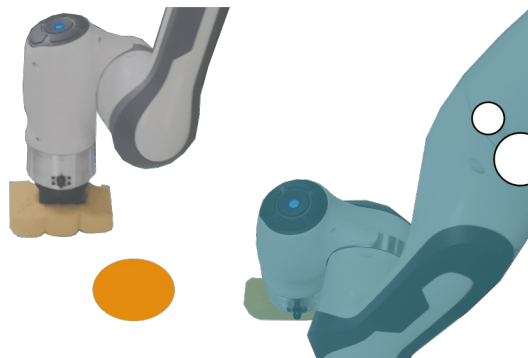
z^k



I think it will
aim right
next



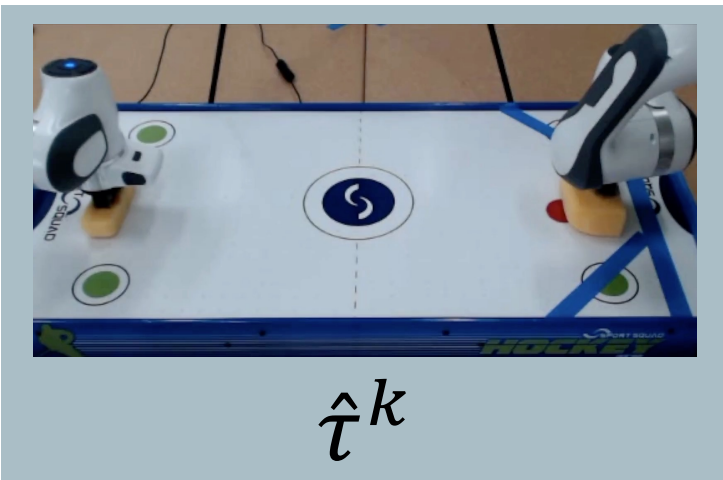
z^k

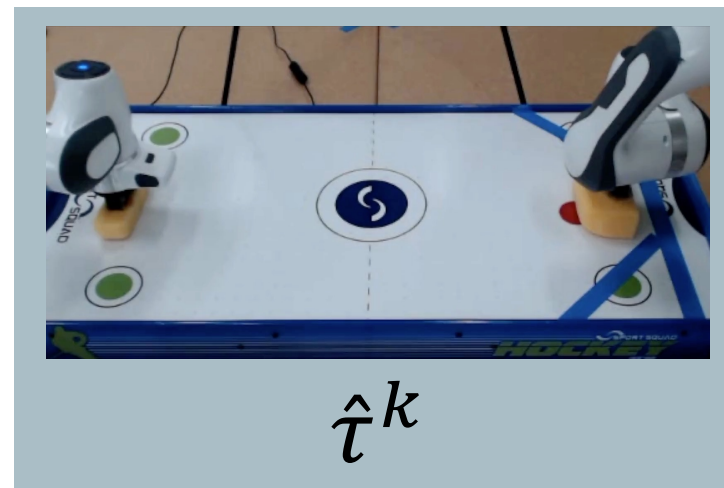
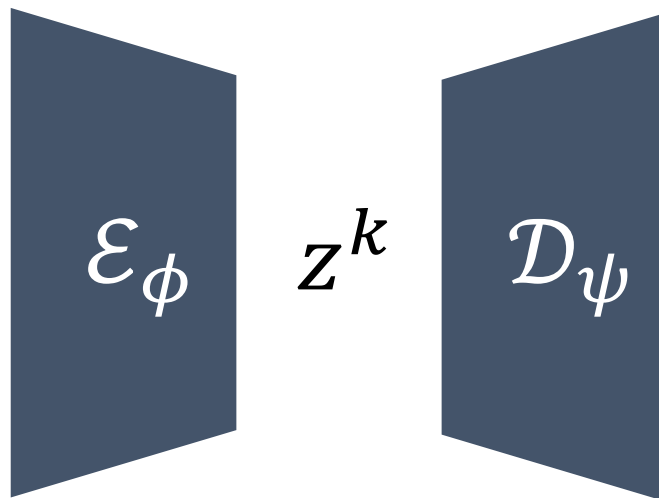
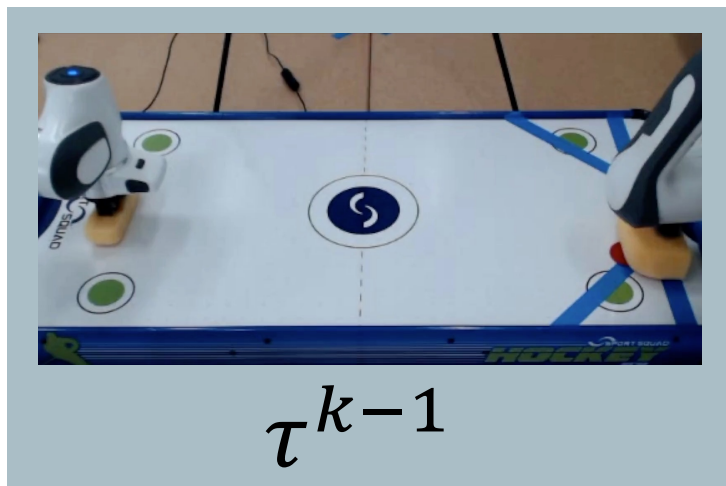
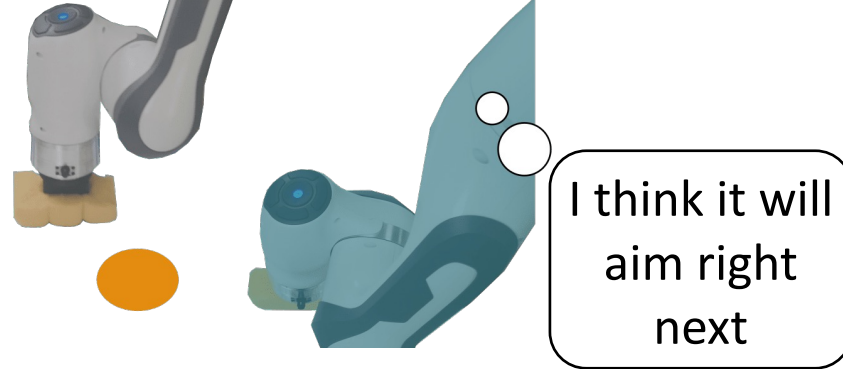


I think it will aim right next



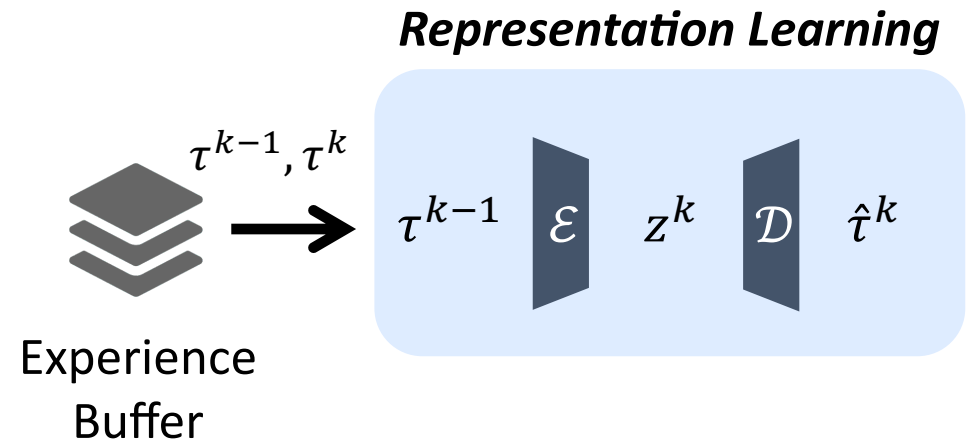
z^k





Learning objective:

$$\max_{\phi, \psi} \sum_{i=2}^N \sum_{t=1}^H \log p_{\phi, \psi}(s_{t+1}^i, r_t^i \mid s_t^i, a_t^i, \tau^{i-1})$$

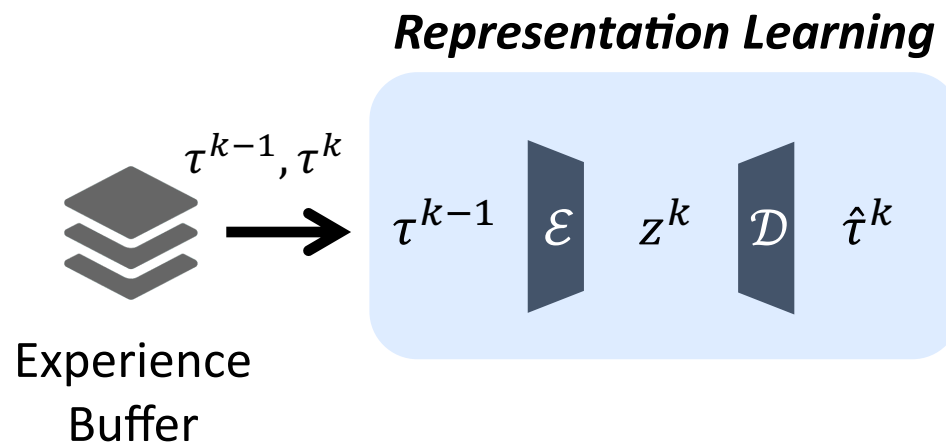


Learning and Influencing Latent Intent

Maximize expected return
within an interaction

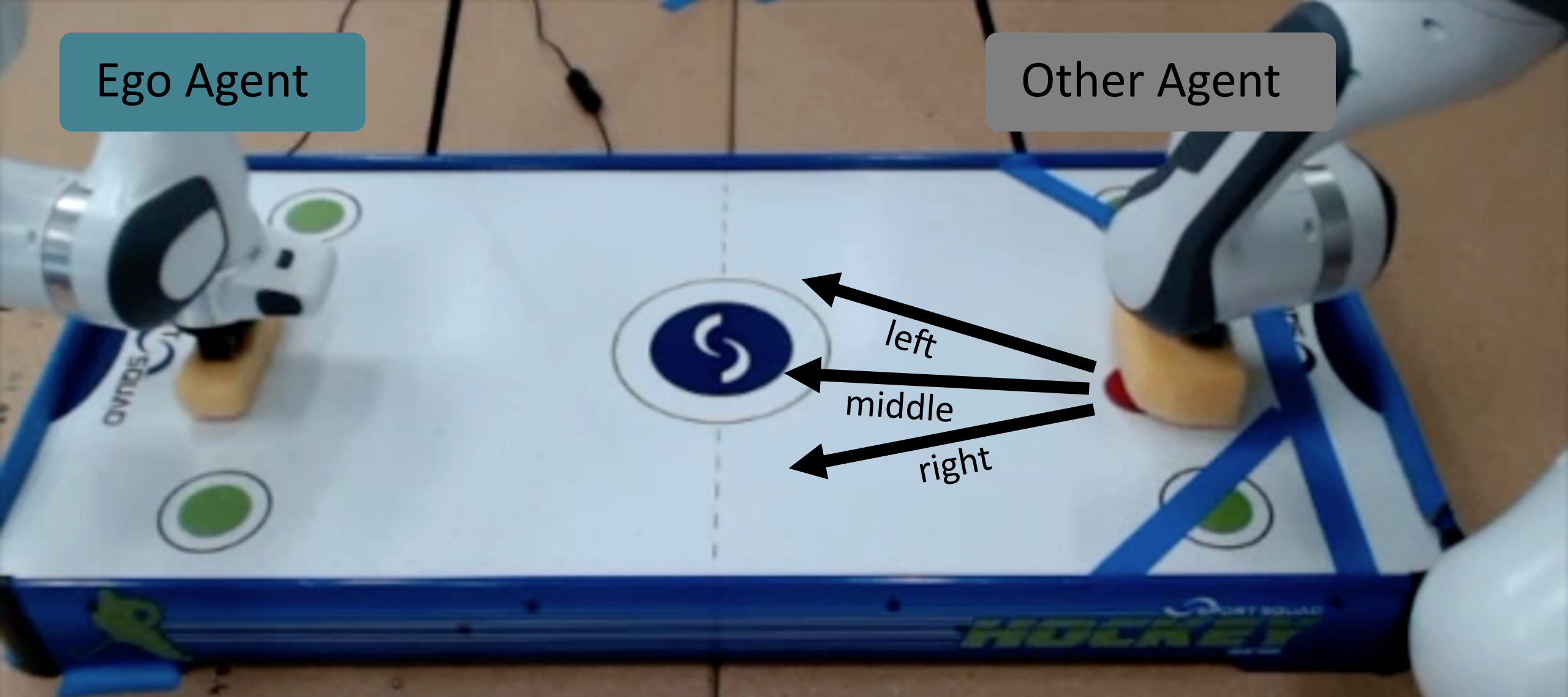
$$\max_{\theta} \mathbb{E}_{\pi_{\theta}(a|s, z^i)} \left[\sum_{t=1}^H R(s, z^i) \right]$$

to *react* to the other agent



Ego Agent

Other Agent



Air Hockey Results

Ego Agent

+1

Other Agent



Air Hockey Results

Ego Agent

Other Agent



Air Hockey Results

Ego Agent

+2

Other Agent



Air Hockey Results

Ego Agent

Other Agent



Air Hockey Results

2x speed



SAC: initial policy

2x speed



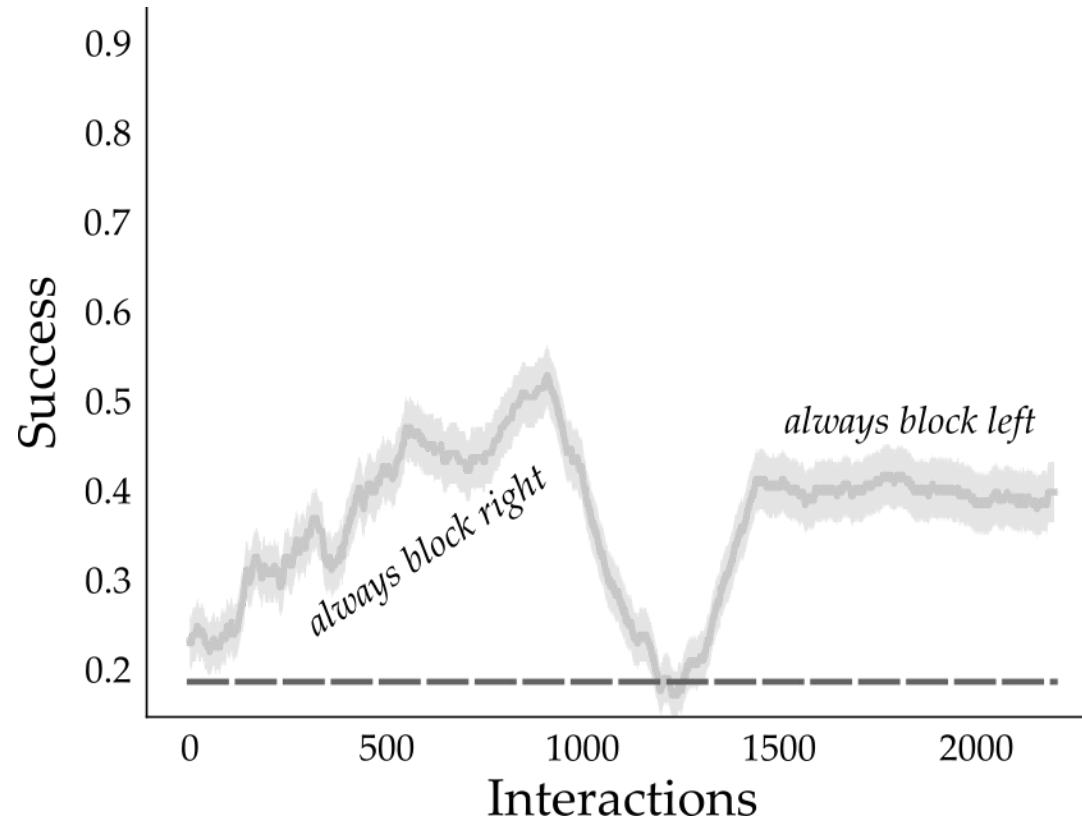
SAC: 2 hours of training

2x speed



SAC: 4 hours of training

Air Hockey Results



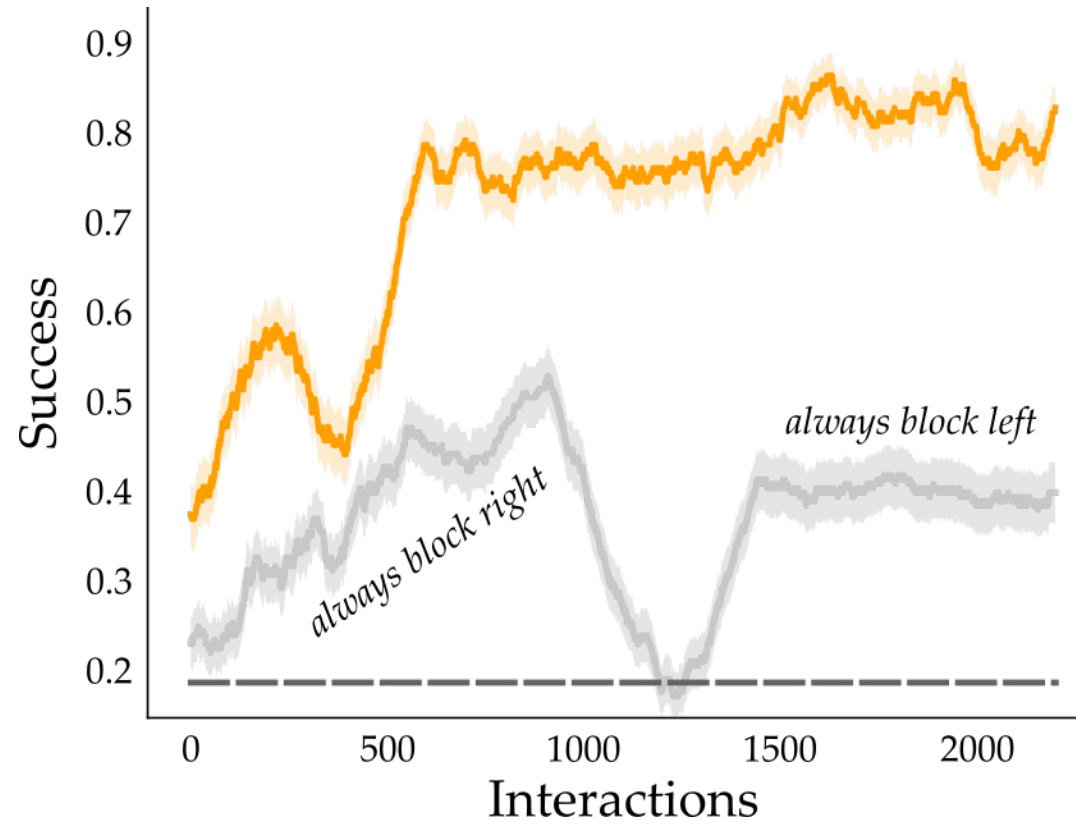
■ Random ■ SAC ■ LILI

2x speed

LILI: 4 hours of training



Air Hockey Results



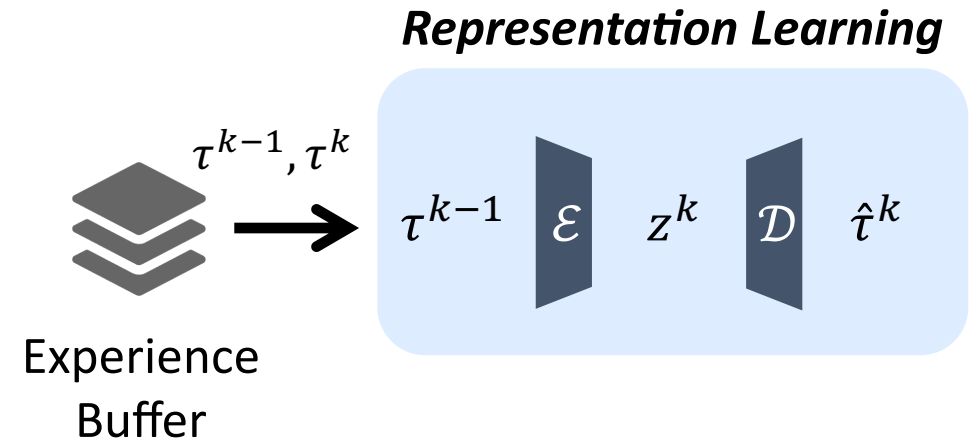
■ Random ■ SAC ■ LILI

Reacting to Other Agents

Maximize expected return
within an interaction

$$\max_{\theta} \mathbb{E}_{\pi_{\theta}(a|s, z^i)} \left[\sum_{t=1}^H R(s, z^i) \right]$$

to *react* to the other agent

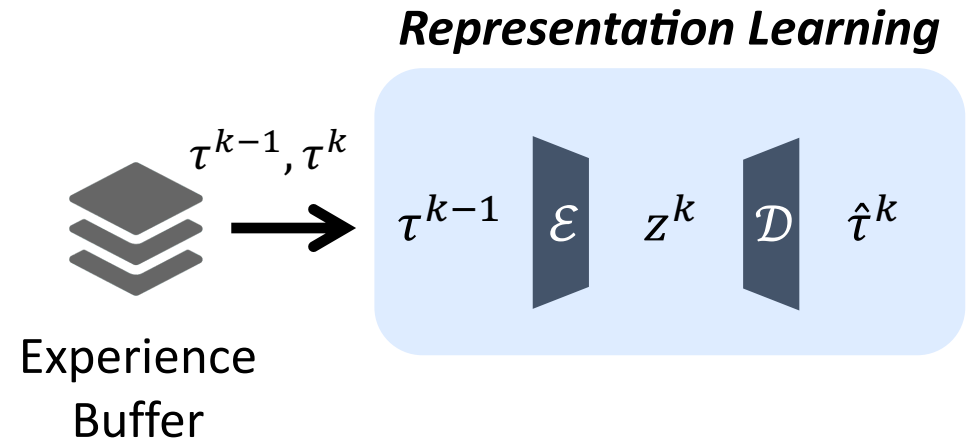


Influencing Other Agents

Maximize expected return *across* interactions

$$\max_{\theta} \sum_{i=1}^{\infty} \gamma^i \mathbb{E}_{\pi_{\theta}(a|s, z^i)} \left[\sum_{t=1}^H R(s, z^i) \right]$$

to *influence* the other agent

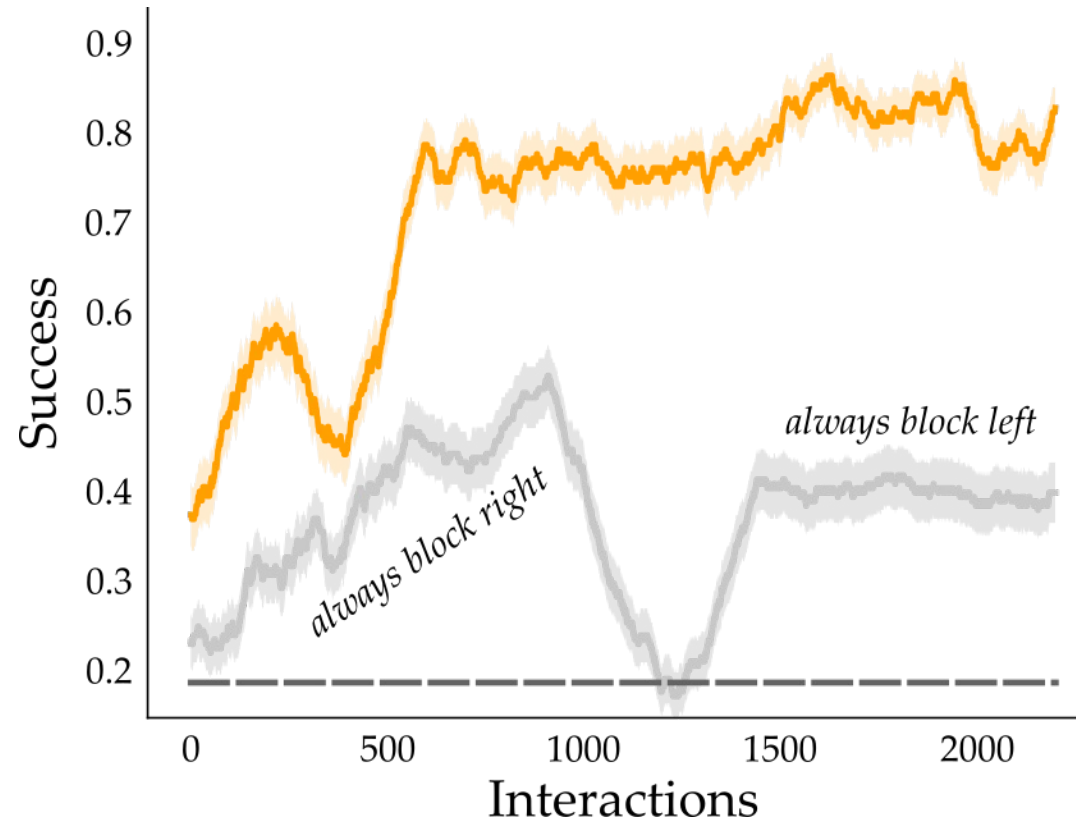




2x speed

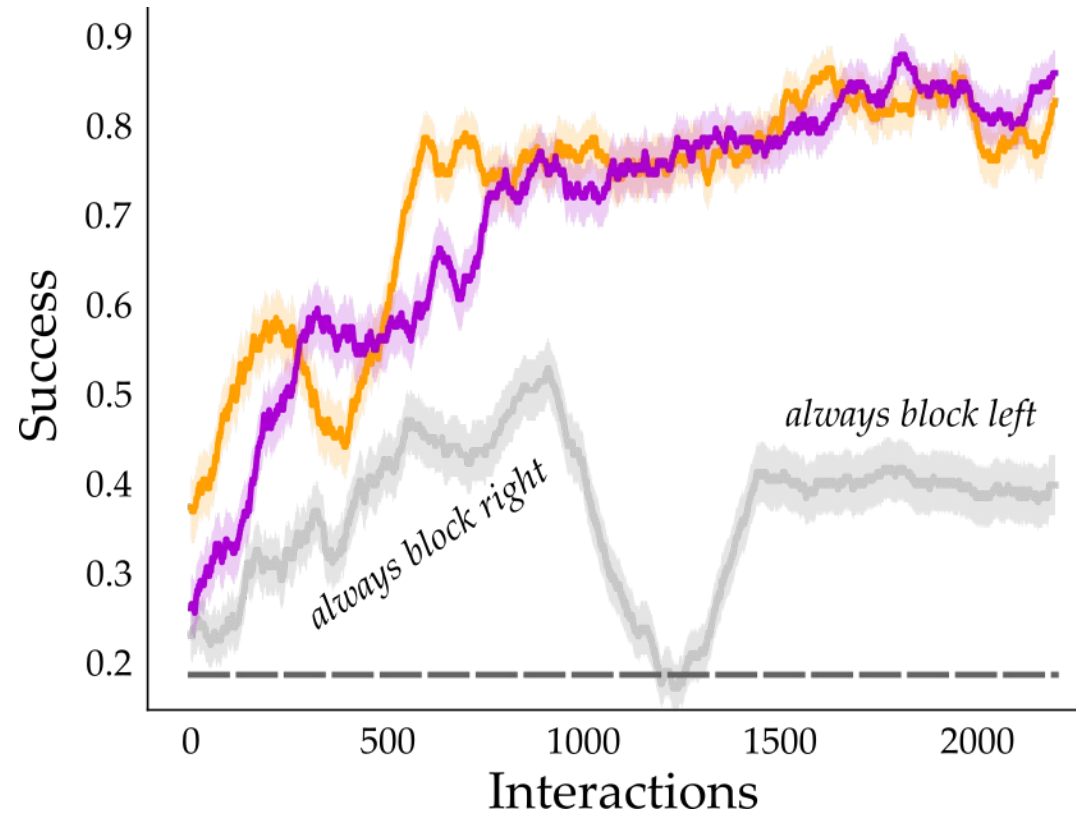
LILI (with influence): 4 hours of training

Air Hockey Results



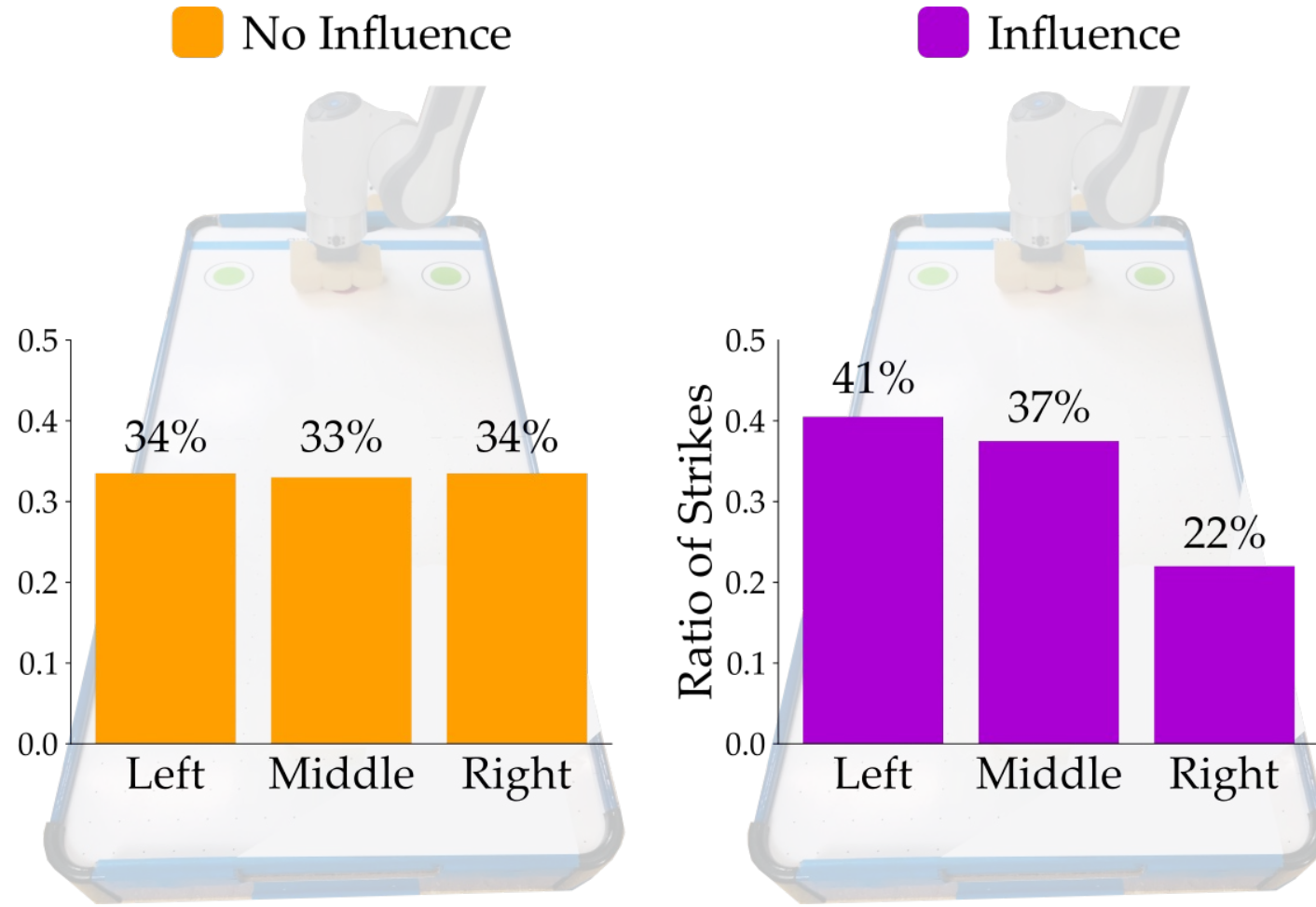
■ Random ■ SAC ■ LILI (no influence) ■ LILI (ours)

Air Hockey Results



■ Random ■ SAC ■ LILI (no influence) ■ LILI (ours)

Air Hockey Results



Playing with a
Human Expert



SAC: 45% success

Playing with a Human Expert



Key Takeaways

Human partners are often **non-stationary** – which can be represented by low-dimensional **latent strategies**.

LILI *anticipates* the partner's policies using **latent strategies** to *react* and *influence* the other agent.

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