

Principles of Robot Autonomy II  
Exam 3  
March 17, 2023

Name:

SUNet ID:

**Instructions:**

- Time allowed: 60 minutes.
- Total Points: 48.
- The exam consists of **three** problems.
- Please read all questions carefully before answering. Correct answers will receive full credit.
- **To get partial credit for an incorrect answer, you should explain your reasoning.** Please write all your answers in the provided answer sheet.

Good luck!

### 1. Imitation Learning (24 points)

- (i) True or False: Unlike vanilla behavior cloning, the goal of DAgger is to find a policy that matches the feature expectations of the expert demonstrations.
- (ii) You are trying to learn a linear reward function for an RC car that you want to move with a desired speed  $v_{\text{des}}$  when it is safe to do so. The linear reward function has the following form:

$$r(s) = \sum_i \omega_i \phi_i(s)$$

where  $s$  denotes the state, which includes the speed  $v$  of the vehicle along with other information,  $\omega$  is the weight vector, and  $\phi(s)$  is the features associated with state  $s$ . Assume only one of the features carries information about the speed  $v$  of the vehicle. One of your co-workers comes up with a list of possible functions for this speed feature to make the RC car move with  $v_{\text{des}}$ :

$$v, \quad v - v_{\text{des}}, \quad |v - v_{\text{des}}|, \quad \mathbb{I}(v \geq v_{\text{des}}), \quad \exp\left(-\frac{(v - v_{\text{des}})^2}{2}\right)$$

where  $\mathbb{I}$  is the indicator function. Considering the fact that you are going to learn a linear reward function, which of the following features are reasonable for this task?

$$\begin{aligned} &v \\ &v - v_{\text{des}} \\ &|v - v_{\text{des}}| \\ &\mathbb{I}(v \geq v_{\text{des}}) \\ &\exp\left(-\frac{(v - v_{\text{des}})^2}{2}\right) \end{aligned}$$

*Explain:*

- (iii) True or False: Conditional imitation learning does not suffer from the problem of compounding errors.

- (iv) True or False: In inverse reinforcement learning, there are many reward functions under which the expert demonstrations are optimal.
- (v) True or False: In maximum margin planning, we can account for potential expert suboptimality by introducing a slack variable.
- (vi) Which of the following is **not** an advantage of behavior cloning compared to reinforcement learning?
  - Removes the need for hand-designed reward functions
  - Improves the long-horizon planning
  - Avoids the problem known as reward hacking, in which reinforcement learning agents learn to exploit a reward function instead of the desired behavior

*Explain:*

**Solution:**

- (i) False. Behavior cloning and DAgger aim to match the state-conditioned action distribution of the expert. Matching the feature expectations is the goal of some inverse reinforcement learning algorithms.
- (ii)  $|v - v_{\text{des}}|$  and  $\exp\left(-\frac{(v-v_{\text{des}})^2}{2}\right)$  are reasonable, because  $v = v_{\text{des}}$  either minimizes or maximizes them. For  $v$  and  $v - v_{\text{des}}$ , the car is going to learn either minimizing or maximizing the speed. For  $\mathbb{I}(v \geq v_{\text{des}})$ , the reward will be indifferent between the values that are larger (or smaller) than  $v_{\text{des}}$ .
- (iii) False. Conditioning on the user goal alone will not address the problem of compounding error in imitation learning.
- (iv) True. Reward ambiguity is an issue for IRL where multiple policies may lead to the same reward function.
- (v) True.
- (vi) Improves the long horizon planning. Behavior cloning does not perform long-horizon planning and actually suffers from compounding errors.

**2. Learning from Diverse Sources of Data (12 points)**

- (i) True or False: Learned reward functions that are modeled with linear models are less expressive than those modeled with neural networks, because they consider only linear combinations of a predefined set of features.
  
- (ii) True or False: In active preference-based learning, the agent chooses a pair of trajectories for a human to compare based on the human's responses to previous queries.
  
- (iii) There are many forms of human feedback that robots can learn from, such as
  - Offline expert demonstrations
  - Interactive expert demonstrations
  - Suboptimal demonstrations
  - Physical corrections
  - Pairwise comparisons of trajectories
  - Large language models

Select one form of feedback from the list and answer the following questions:

- What is a pro and a con of this form of feedback?
- In one sentence, what is the key idea of the algorithm that leverages this form of feedback?
- Is the algorithm an example of direct policy learning or reward learning?

*Explain:*

**Solutions:**

- (i) True.
- (ii) True. The agent generates an informative query for the human to compare two trajectories given how the human has responded to the previous queries so far.
- (iii) Various correct answers.

### 3. Interaction-aware control and shared autonomy (12 points)

- (i) When modeling interactions between humans and robots in a game-theoretic fashion (theory of mind), we often struggle with the computational challenges of recursive belief modeling. Can you provide one way of addressing such computational challenges?

*Explain:*

- (ii) An autonomous car with a limited-range camera is driving on a road that may have a 30-mph speed limit. It uses a POMDP to model the problem. Suppose the POMDP includes 1) two states  $\mathcal{S} = \{0, 1\}$ , representing whether the road has a 30-mph speed limit; 2) two observations  $\mathcal{O} = \{0, 1\}$  representing whether the robot sees a speed limit sign; 3) a continuous action set  $\mathcal{A} = [0, 60]$  representing the speed of the autonomous car. Assume the initial state distribution is uniform over  $\mathcal{S}$ . Let the transitions, observations and reward be modeled as:

$$P(s' | s, a) = \mathbb{I}(s' = s)$$

$$P(o | s) = \begin{cases} \frac{1}{2} & \text{if } s = 1, \\ 1 & \text{if } s = o = 0, \\ 0 & \text{otherwise.} \end{cases}$$

$$R(s, a, s') = -s(a - 30)^2 - (1 - s)(a - 60)^2$$

for  $\forall s, s' \in \mathcal{S}, \forall o \in \mathcal{O}, \forall a \in \mathcal{A}$ . What is the optimal action when  $o = 0$ ?

- 0
- 20
- 30
- 50
- 60

*Explain:*

- (iii) True or False: Q-MDP is a method that always gives the exact solution to POMDPs.

#### Solutions:

- (i) Various correct answers, including approximating the game using a Stackelberg game (leader-follower game) and bringing down dimensionality of the action space by operating in the latent intent space.
- (ii) (d). When  $s = 0$ , we have  $o = 0$  with probability 1. When  $s = 1$ , we have  $o = 0$  with probability  $1/2$ . By Bayes' rule,  $s = 0$  with probability  $2/3$  when  $o = 0$ . Since changing the state is not ever possible in this POMDP, we just need to maximize the immediate reward. Solving  $a^* = \arg \max_a -\frac{2}{3}(a - 30)^2 - \frac{1}{3}(a - 60)^2$  gives  $a^* = 50$ .
- (iii) False. QMDP only attempts to approximate the solution to POMDPs by assuming that full observability will be attained in the next time step.